

# Hard Exclusive Reactions

$\gamma$

Caroline Riedl



$\varrho$

J/ $\Psi$

$\xi$

$\eta$

Milos, Greece, 30.9.2009

$\omega$

$\phi$

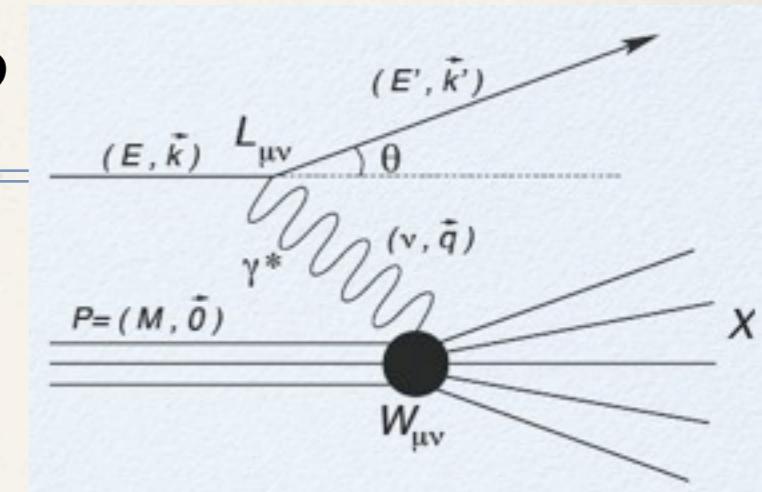
$\pi$

$\Upsilon$

# Outline: Hard Exclusive Reactions

Hard scale:  
 $Q^2$ , M, and/or t

Complete spectrum  
of X known



- Photoproduction ( $Q^2 < 1 \text{ GeV}^2$ )
  - Cross sections ( $Q^2, W, t$ )

testing ground for QCD

- Electroproduction ( $Q^2 > 1 \text{ GeV}^2$ )

- t slopes
- Azimuthal asymmetries
- Spin density matrix elements

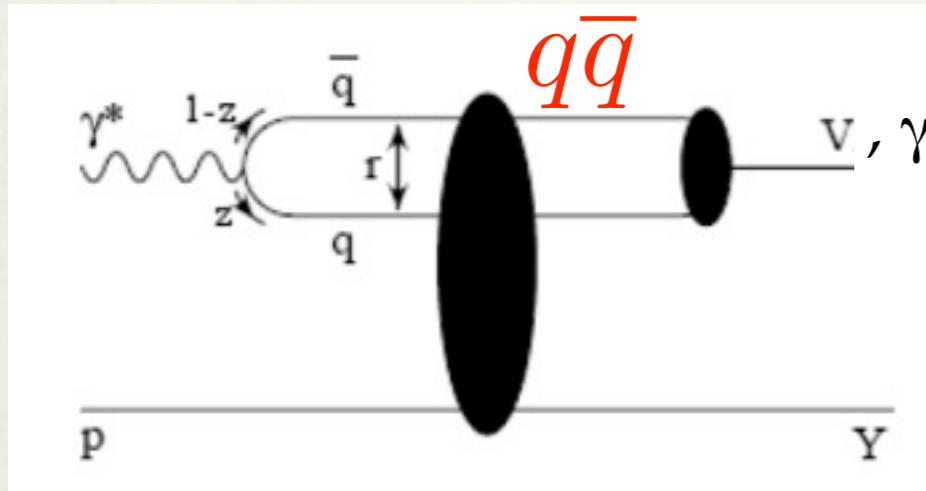
GPDs

total angular  
momentum of quarks

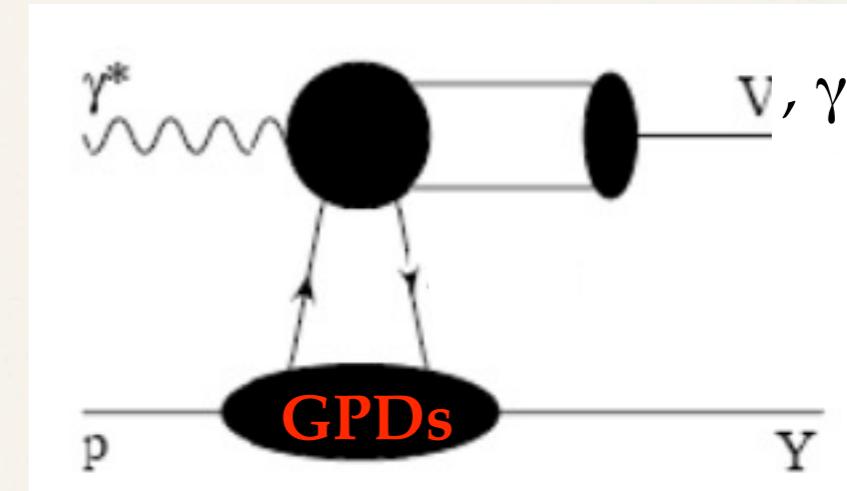
- Future

# $\text{ep} \rightarrow \text{epV}$ or $\text{ep} \rightarrow \text{epy}$ (DVCS)

## High energy factorization



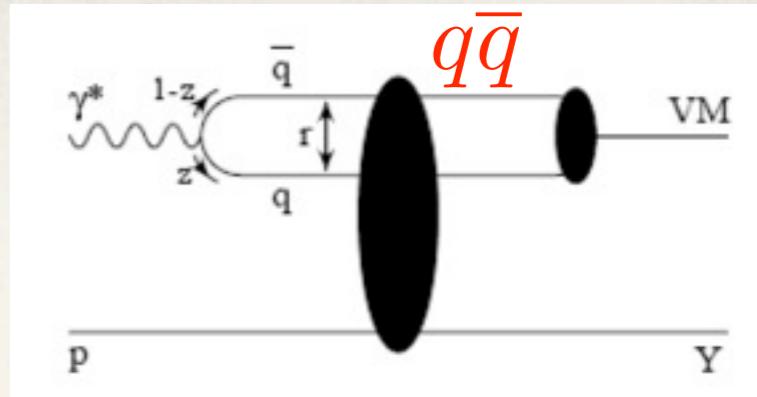
## Collinear factorization



- Universal dipole interactions
- Low  $x \leftrightarrow$  large  $W$
- Scale:  $Q^2 + m_V^2$

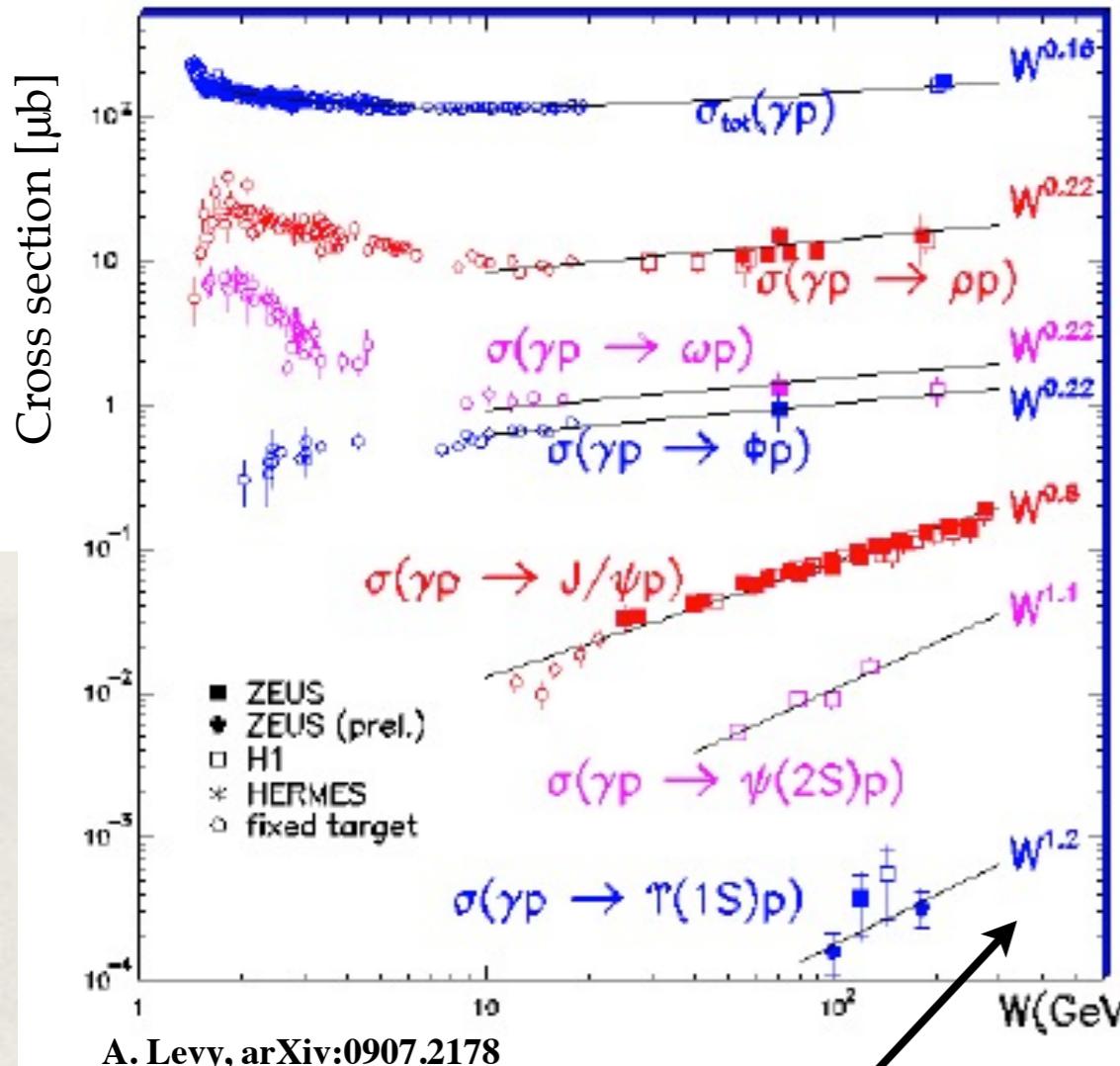
- Parameterization of non-perturbative nucleonic structure
- Information on parton-parton correlations
- VM: proven only for  $\sigma_{\text{Longitudinal}}$

# Kinematic Landscape



# Photoproduction

ep → epV



$$d\sigma/dt \propto [xg(x,Q^2)]^2$$

$q\bar{q}$   
size

$\delta=0.2$

# SOFT Regge, soft pomeron exchange

J/Ψ, γ

δ≥0.8

# HARD pQCD, 2-gluon exchange

M<sub>v</sub>,  
 $\langle W \rangle$

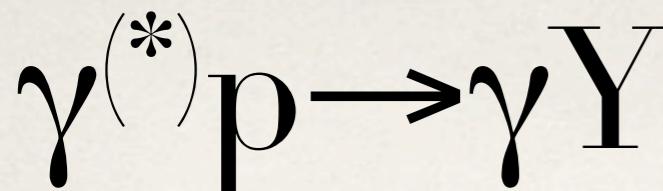
$$d\sigma/dt \propto \exp(-b|t|)$$

**small**

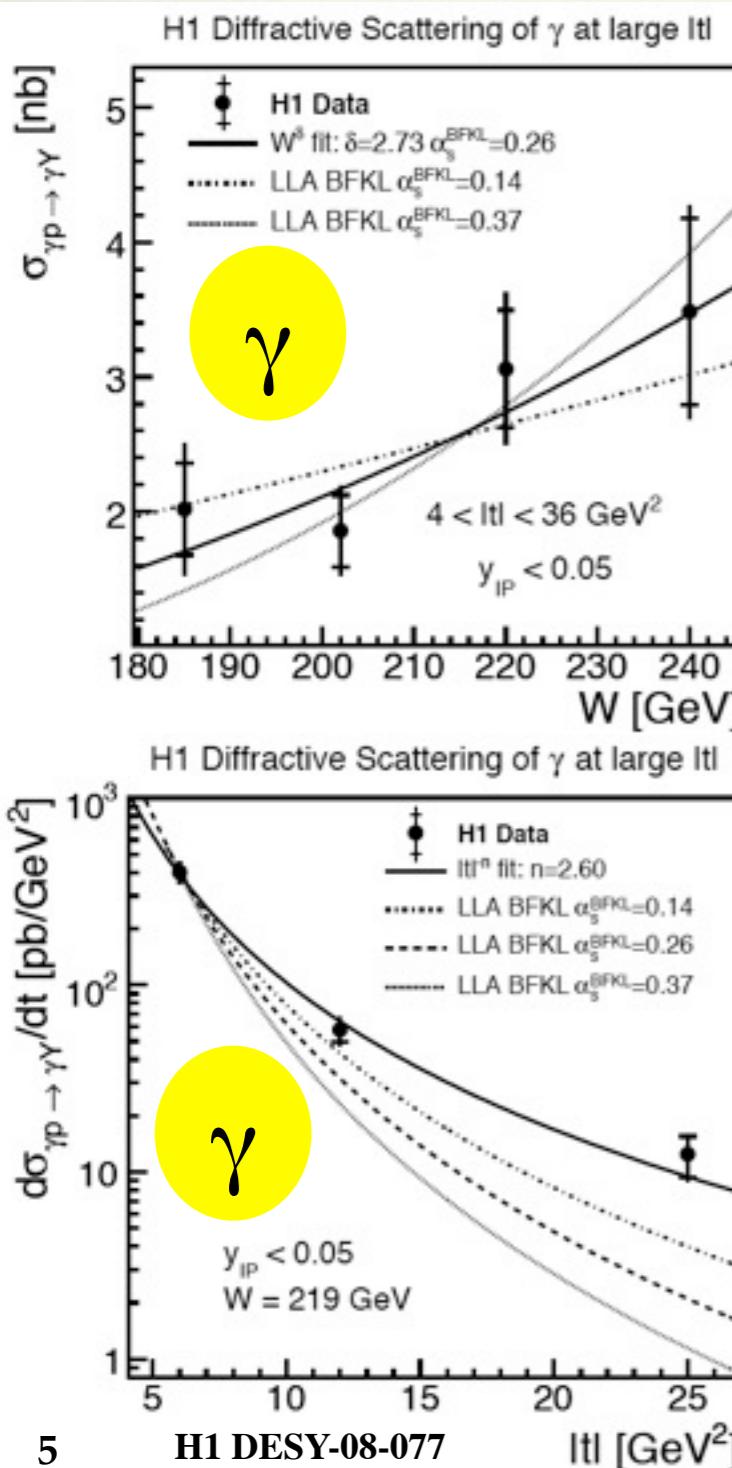
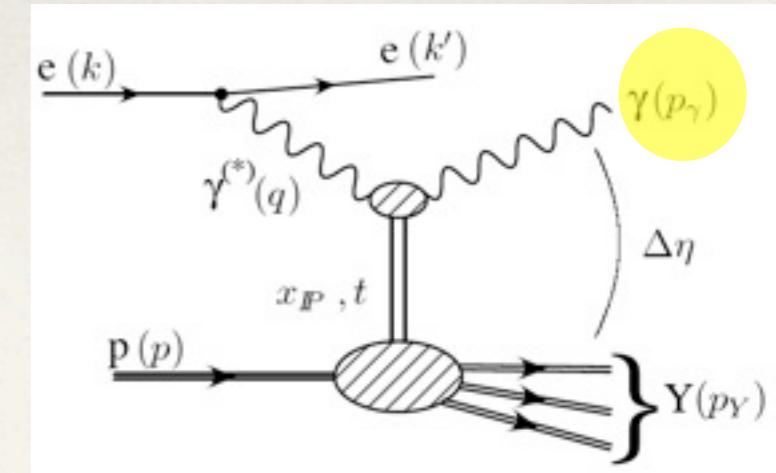
$$\frac{d\sigma}{dt} \propto |t|^{-n}$$

large

10



# Photoproduction



- Large  $|t|$ ,  
proton-dissociative

- $\sigma(W) \propto W^\delta$

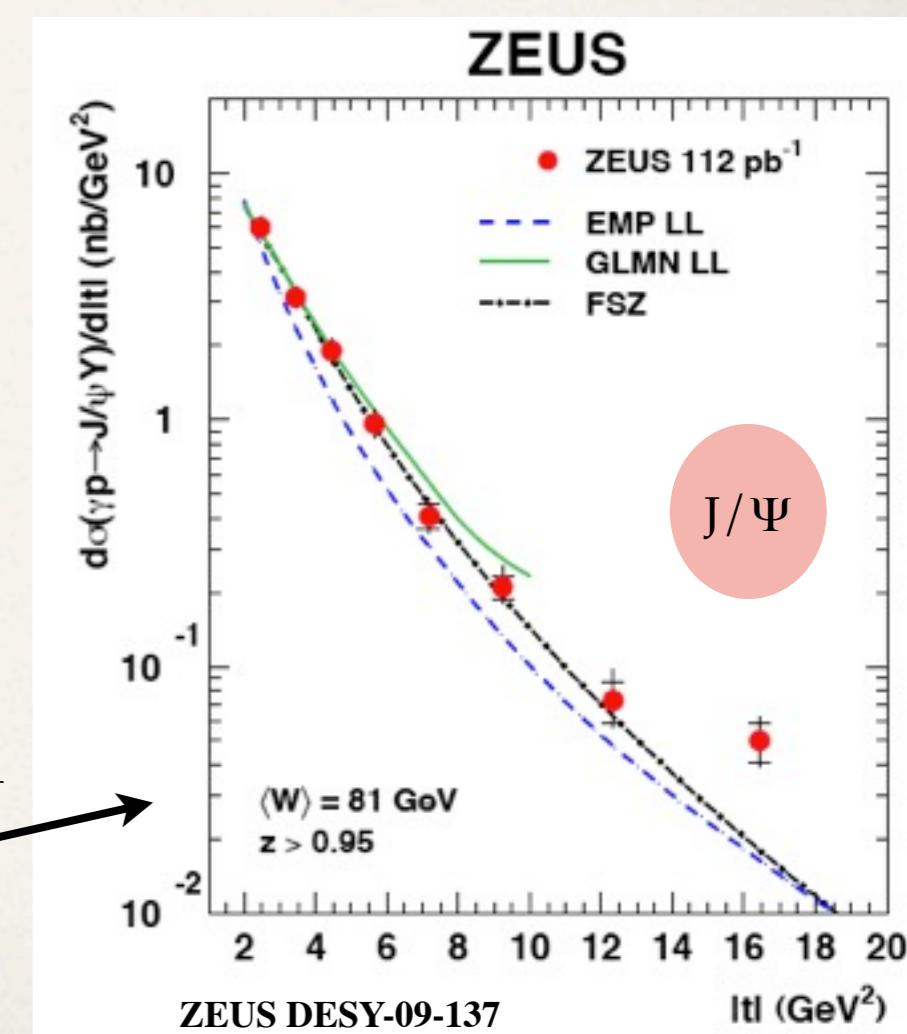
- pQCD: good description

- Compatible with  $J/\Psi$

- $d\sigma / dt \propto |t|^{-n}$

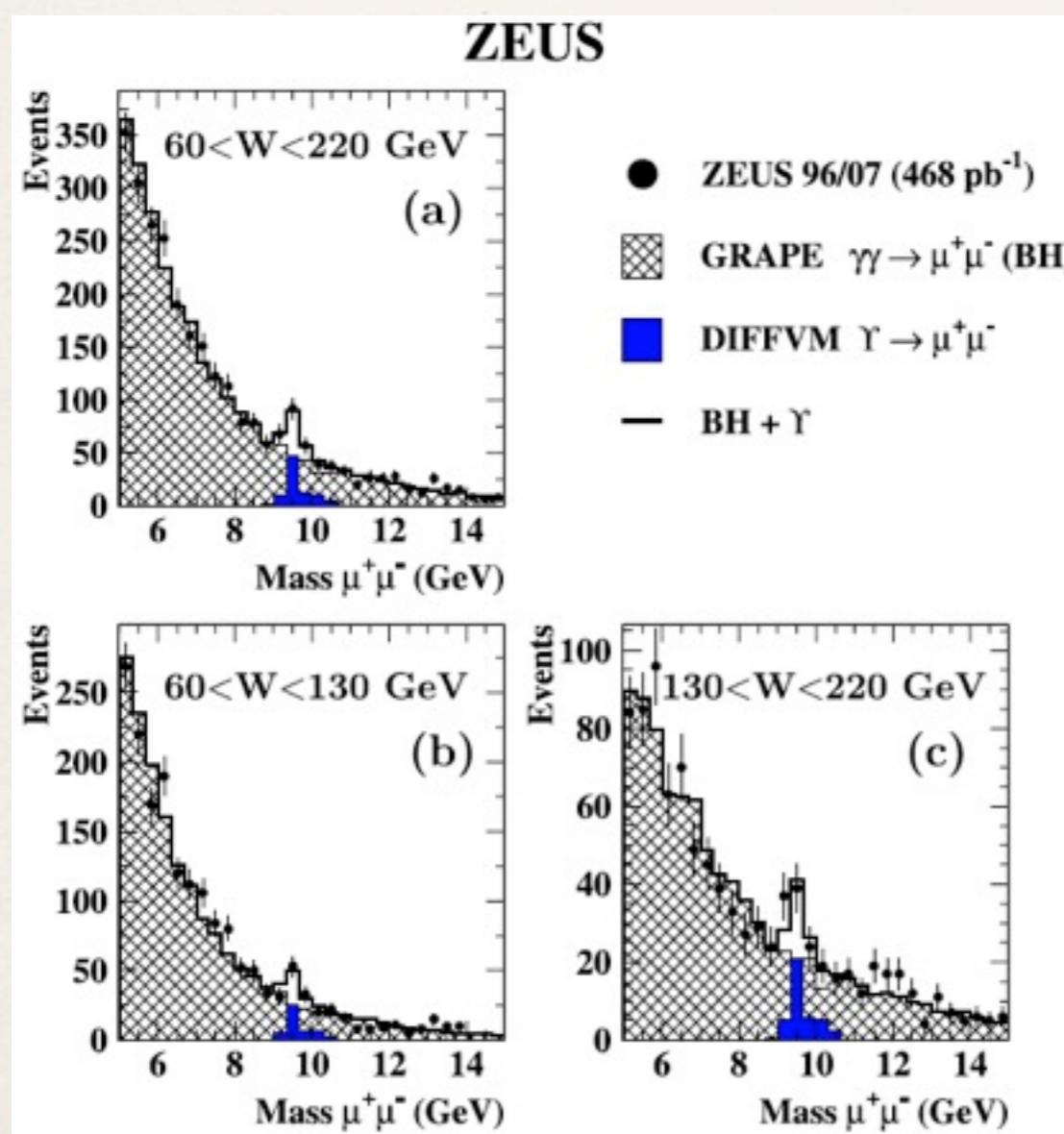
- pQCD: too soft prediction

- Harder than  $J/\Psi$

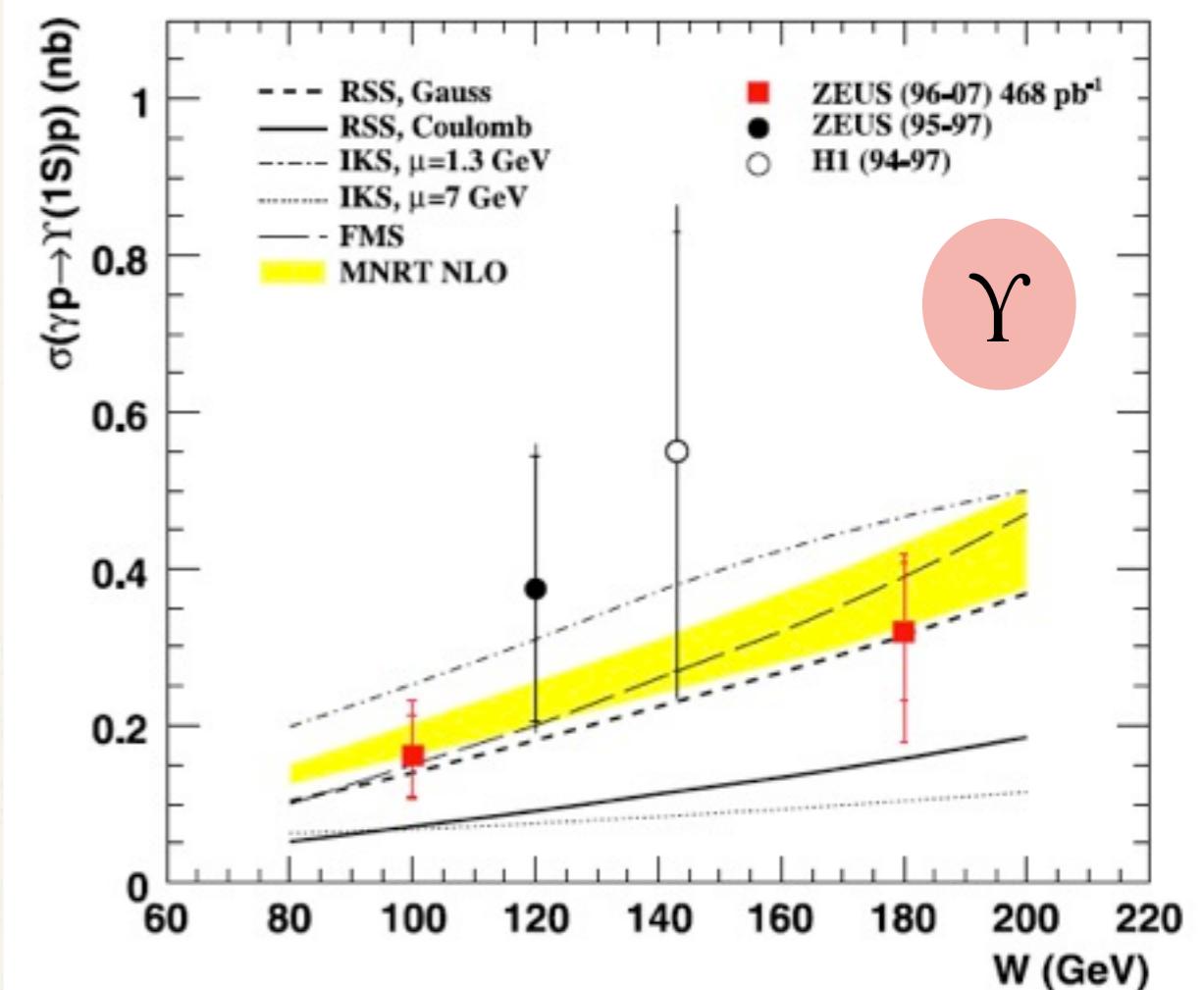


# $e p \rightarrow e p \Upsilon(1S)$ Photoproduction

Di-muon events, invariant mass:



ZEUS 1996-2007, Phys. Lett. B 680 (2009) 4–12

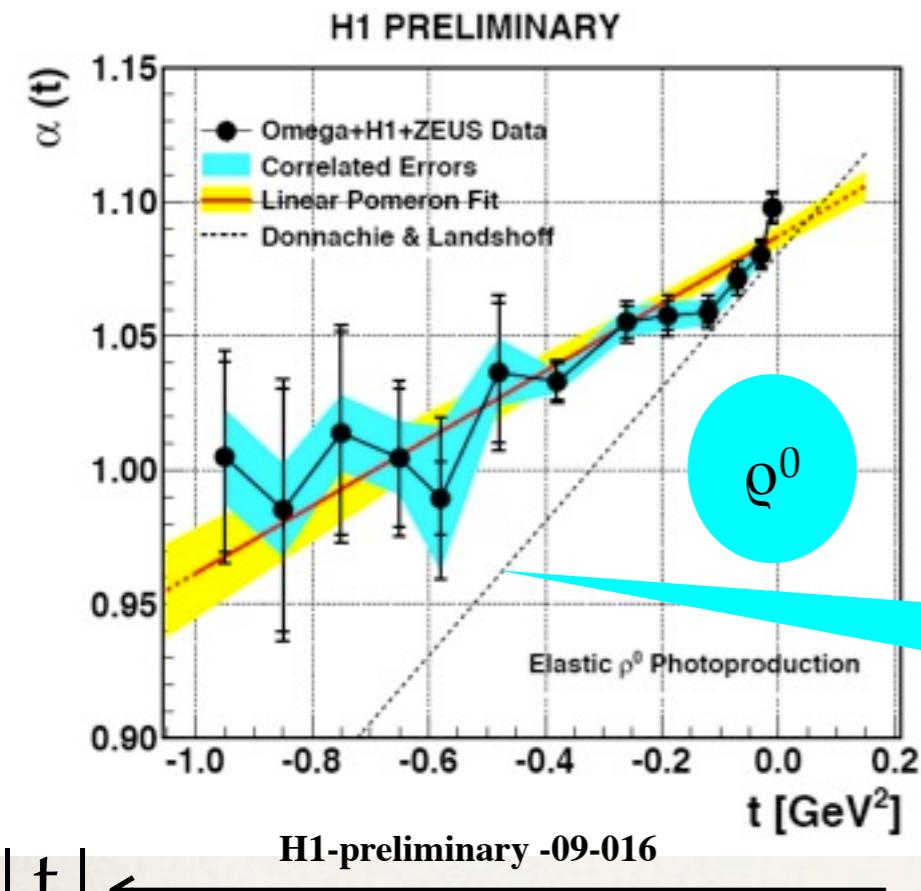


$\sigma \propto W^\delta, \quad \delta = 1.2 \pm 0.8$

pQCD calculations

# $e p \rightarrow e p V$ Pomeron trajectories

## photoproduction light VM



$$d\sigma/dt = F(t) W^{4(\alpha_{IP}(t)-1)}$$

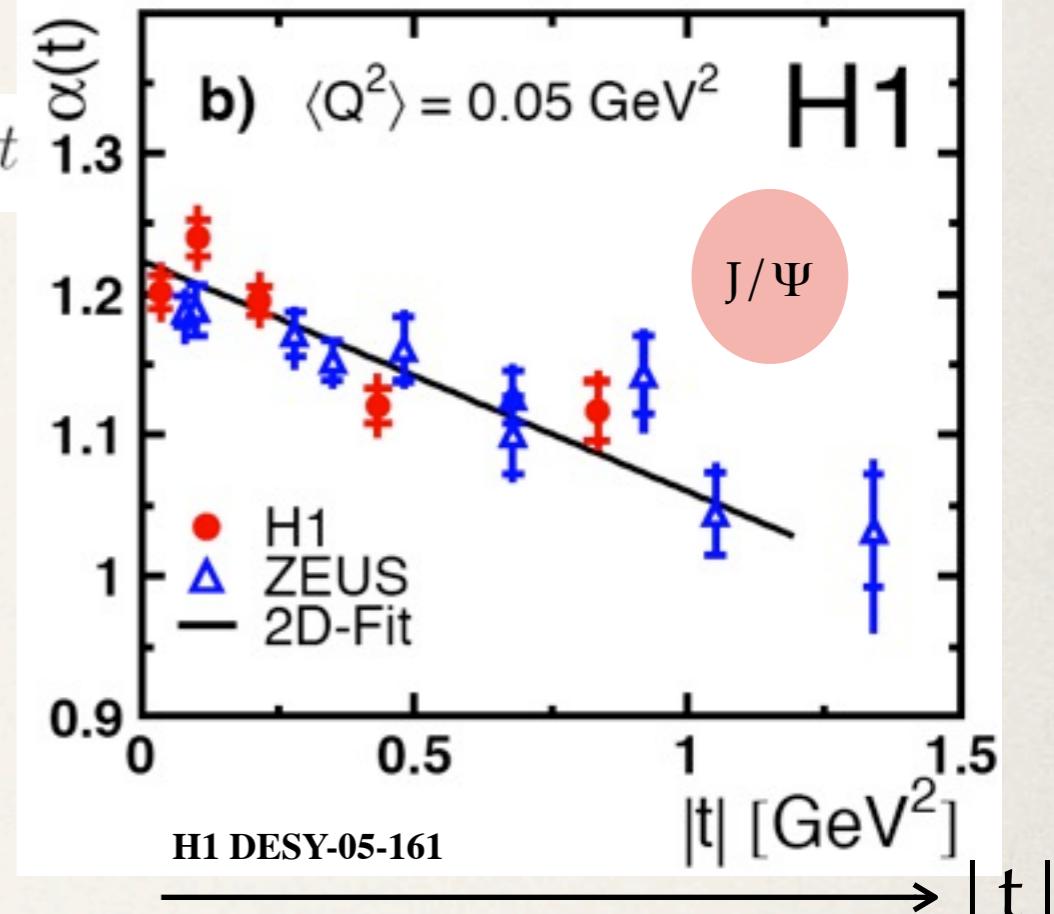
$$\alpha_{IP}(t) = \alpha_{IP}(0) + \alpha'_{IP} \cdot t$$

Canonical soft pomeron:  
 $\alpha'_{IP} = 0.25 \text{ GeV}^{-2}$

$$\alpha'_{IP} = (0.126 \pm 0.013 \pm 0.012) \text{ GeV}^{-2}$$

smaller than canonical soft pomeron

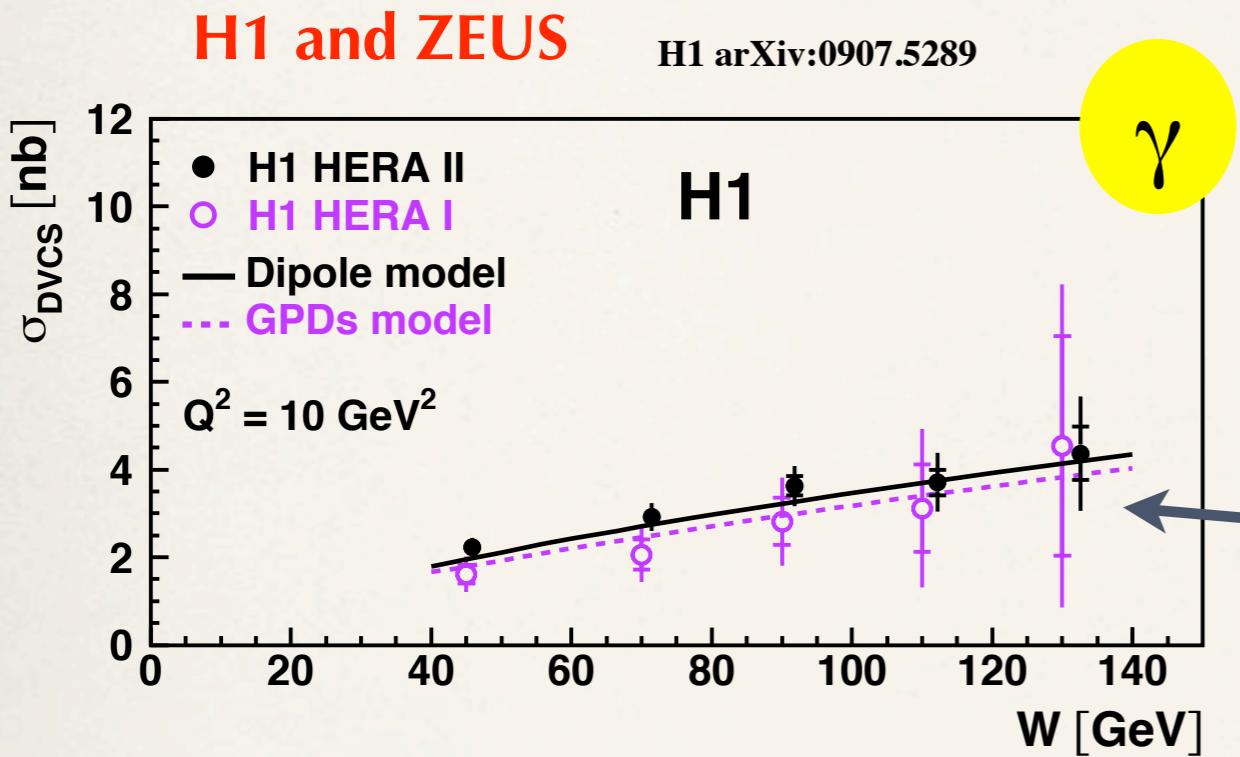
## photoproduction heavy VM



$$\alpha'_{IP} = (0.164 \pm 0.028 \pm 0.030) \text{ GeV}^{-2}$$

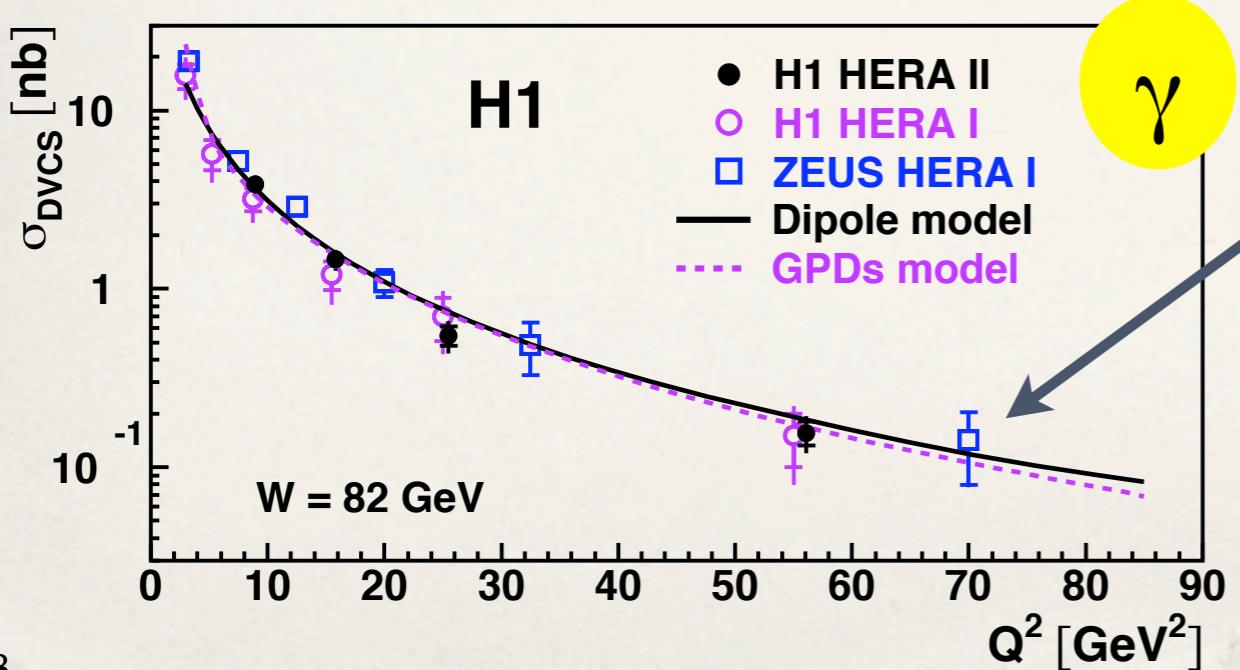
hard pomeron known to be smaller  
 than canonical soft pomeron

# $e p \rightarrow e p \gamma$ cross-section



**Hard exclusive electroproduction of a real photon:  
Deeply Virtual Compton Scattering,  
DVCS**

- Steep  $W^\delta$  dependence
- $\delta \approx 0.7$ , independent of  $Q^2$
- DVCS is a hard process: gluons resolved



- Decrease of  $\sigma_{DVCS}$  with  $Q^2$
- $Q^{2n}$  dependence,  $n \approx 1.5$
- Slower than for vector mesons

# Transverse extension of partons

HERA: DVCS cross section  
differential in  $t$

- Extract  $d\sigma/dt$  in bins of  $Q^2$  and  $W$

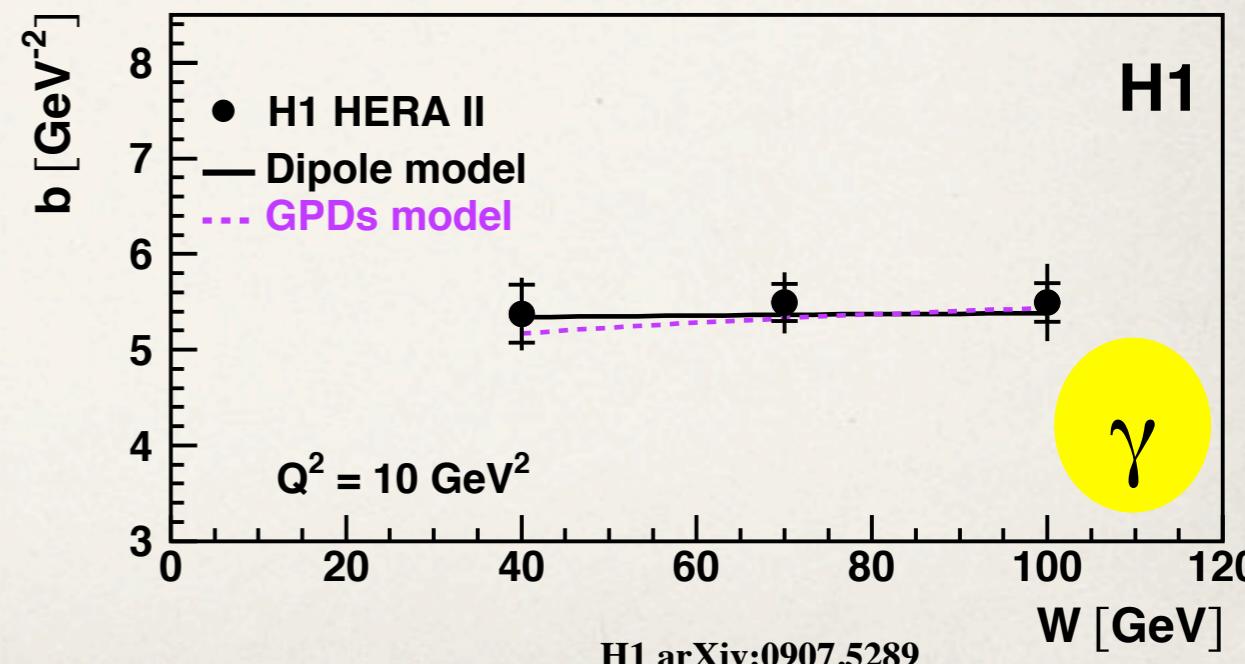
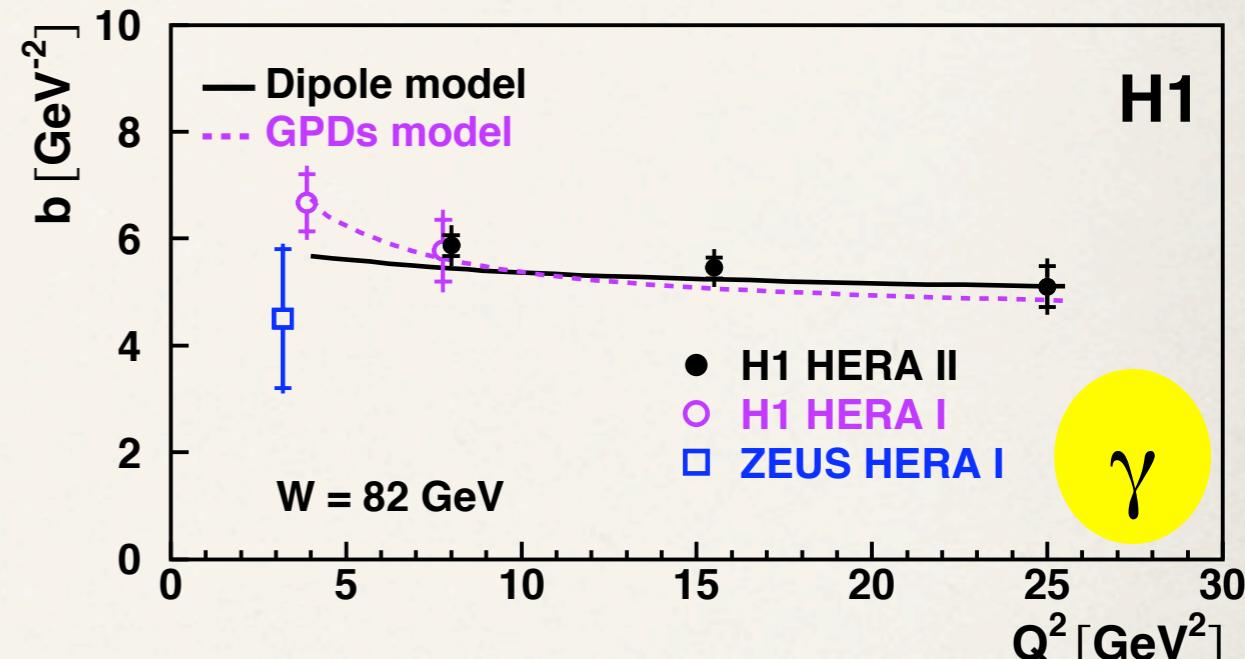
- Ansatz  $d\sigma/dt \propto \exp(-b|t|)$

- $t$  slope  $\rightarrow$  average impact parameter  $b$

- Description of transverse extension of partons

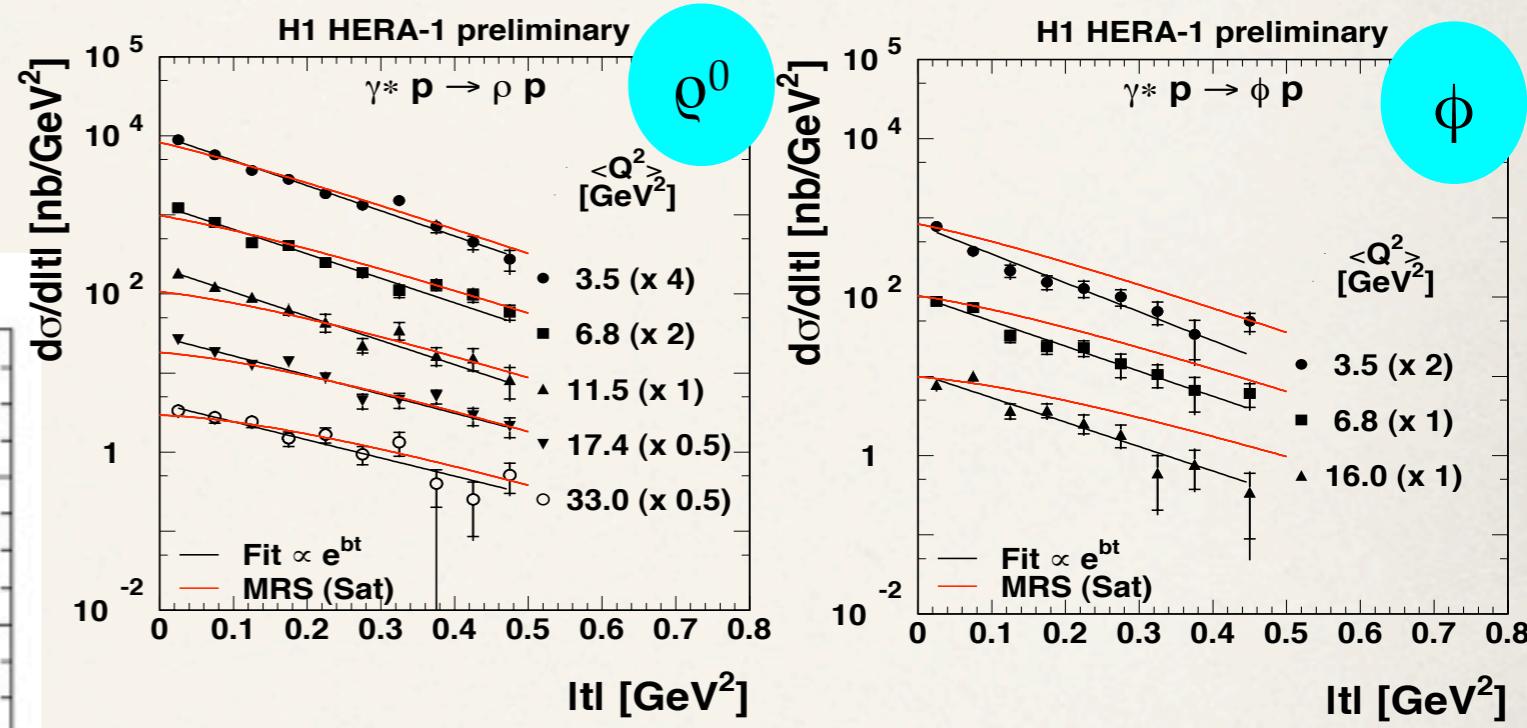
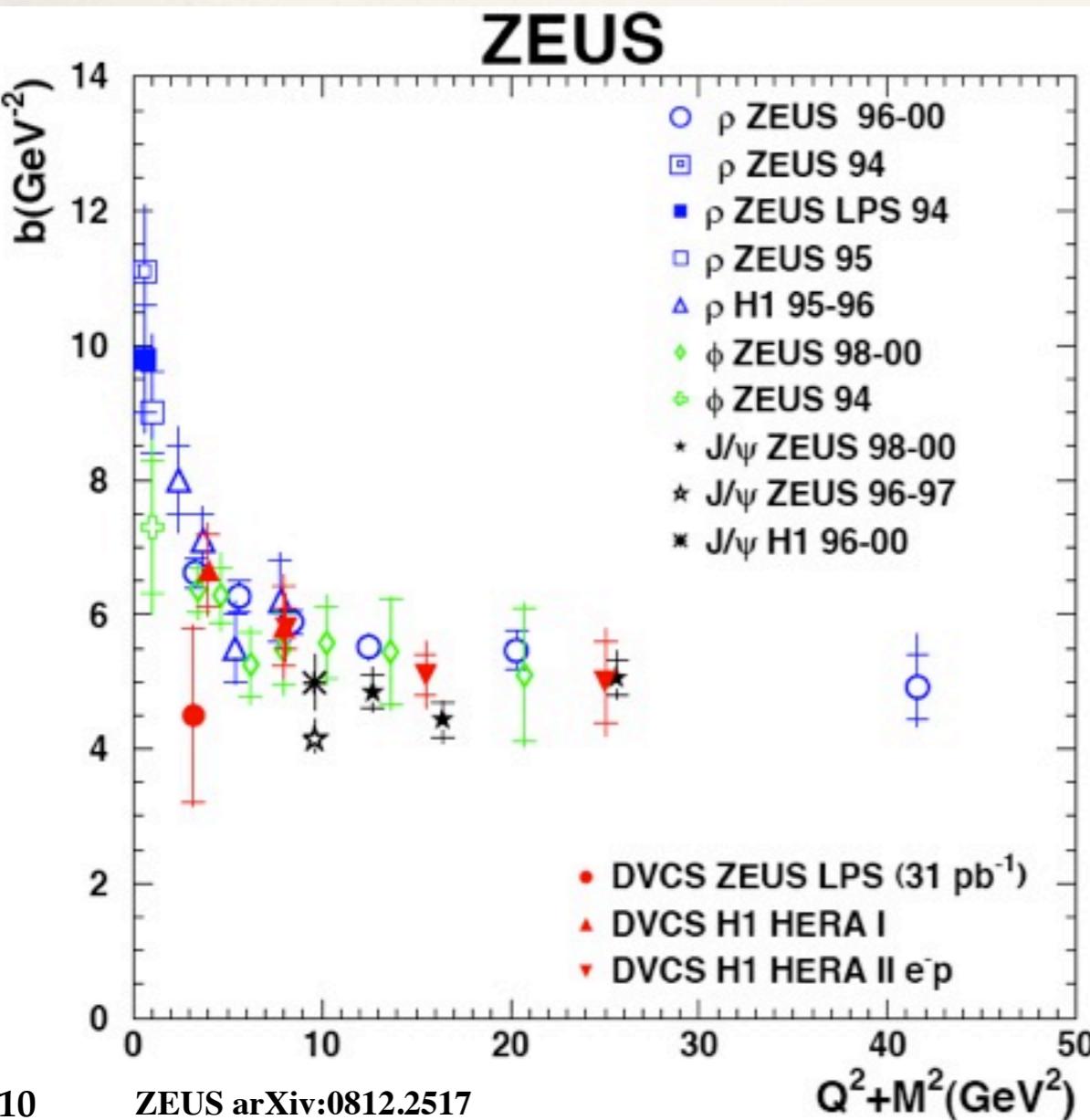
- Size of proton core (w/o soft periphery)

$$\sqrt{\langle r_T^2 \rangle} = (0.65 \pm 0.02) \text{ fm} \quad \text{at } x_B = 10^{-3}$$



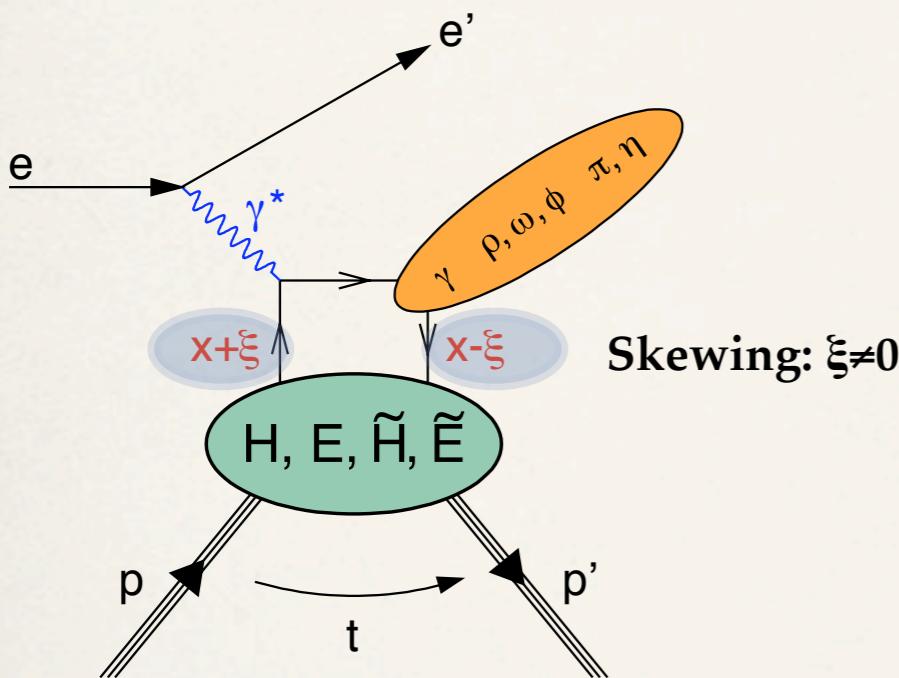
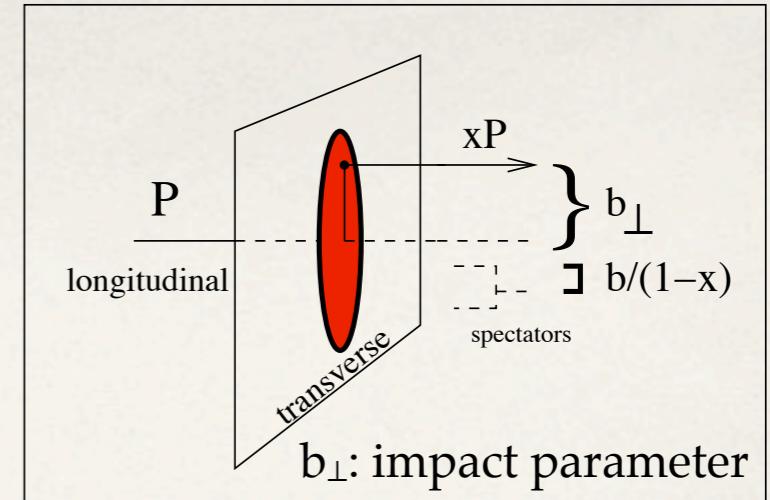
# HERA: t slopes

Electroproduction  
 $ep \rightarrow epV$



- ➊  $b$  measures transverse size of VM  $\oplus$  nucleon
- ➋ VM shrinks with increasing photon virtuality
- ➌ Universal value of  $b \approx 5 \text{ GeV}^{-2}$  at large scale

# Generalized Parton Distributions



**"Nucleon tomography"**

• PDFs: longitudinal momentum

forward limit  $\xi=0, t=0$ :  $H^q(x, 0, 0) = q(x)$

• Form Factors: transverse position

moments of GPDs:  $\int_{-1}^1 dx H^q(x, \xi, t) = F_1^q(t)$

leading twist, quark chirality conserving, spin-1/2

f(quark helicity)	✗	✓
nucleon spin flip	photon: $J^P=1^-$ (DVCS)	
	<b>H</b>	<b>~H</b>
	<b>E</b>	<b>~E</b>
	$J^P=1^-$ mesons	$J^P=0^-$ mesons

• Nucleonic Spin: total angular momentum  
Ji relation:

$$J_q = \frac{1}{2} \lim_{t \rightarrow 0} \int_{-1}^1 dx x [H^q(x, \xi, t) + E^q(x, \xi, t)]$$

# Deeply Virtual Compton Scattering

$$\sigma_{\gamma^*\gamma N} \sim \left| \text{DVCS} + \text{Bethe-Heitler (BH)} + \text{DVCS-BH} \right|^2$$

The diagram shows three Feynman-like diagrams. The first, labeled 'DVCS', shows a virtual photon (wavy line) interacting with a nucleon (circle) to produce a real photon (straight line). The second, labeled 'Bethe-Heitler (BH)', shows a virtual photon interacting with a nucleon to produce a real photon, with a red wavy line attached to the virtual photon line. The third, labeled 'DVCS-BH', shows the sum of the first two diagrams, with a red wavy line attached to the virtual photon line of the DVCS term.

$$= |\mathbf{\tau}_{\text{DVCS}}|^2 + |\mathbf{\tau}_{\text{BH}}|^2 + \mathbf{\tau}_{\text{DVCS}} \mathbf{\tau}_{\text{BH}}^* + \mathbf{\tau}_{\text{DVCS}}^* \mathbf{\tau}_{\text{BH}}$$

**DVCS-BH**

**interference term  $\mathcal{I}$**

Contribution at colliders.

Fixed target:

$$|\mathbf{\tau}_{\text{DVCS}}|^2 \ll |\mathbf{\tau}_{\text{BH}}|^2$$

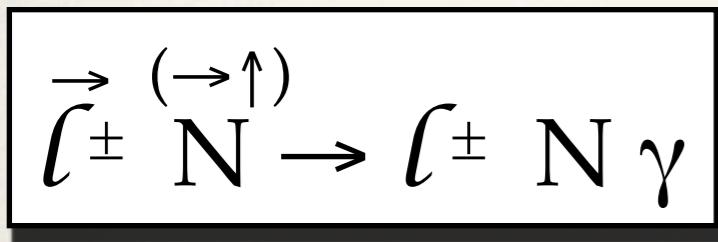
Exactly calculable in QED  
given the nucleon elastic  
form factors  $F_1$  and  $F_2$

Holographic principle:

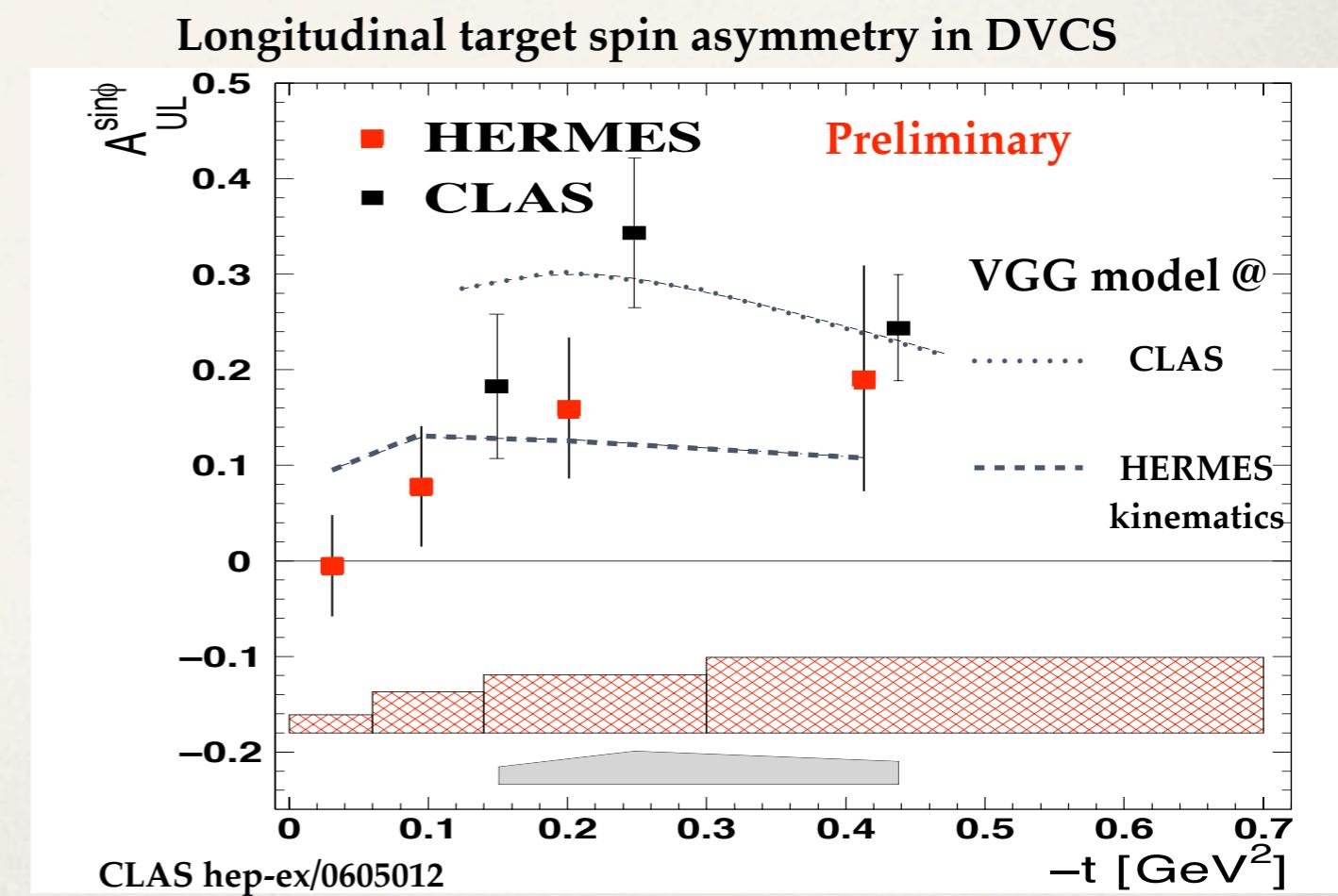
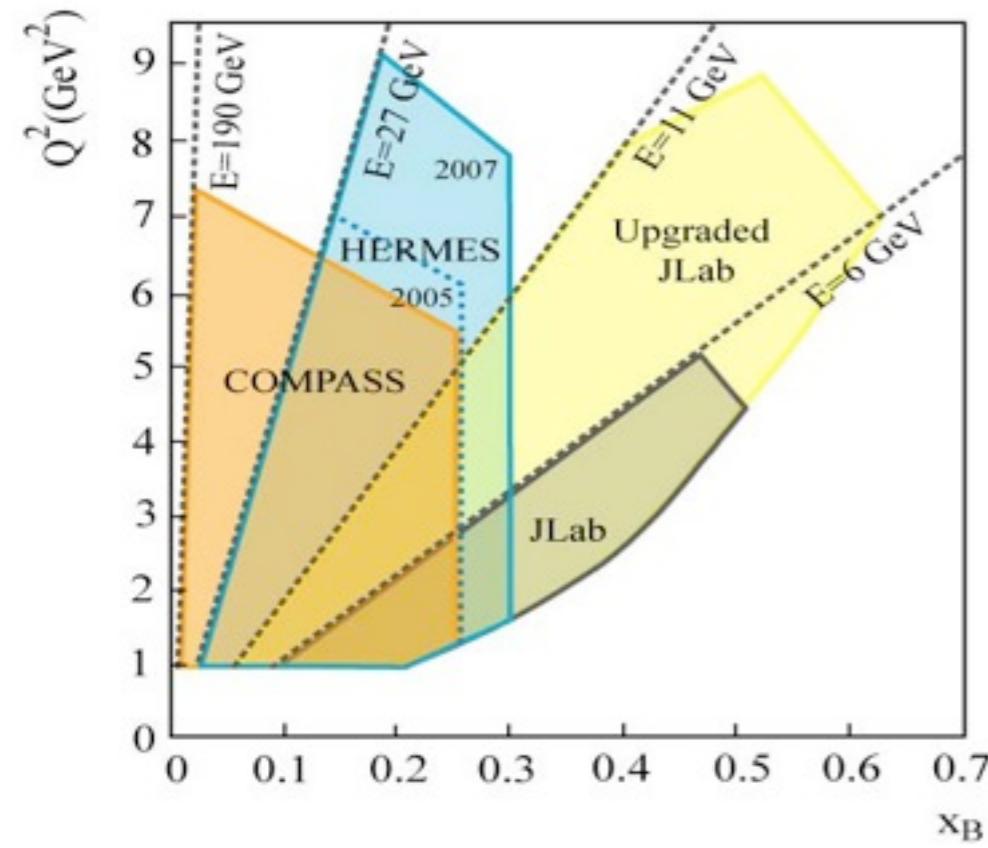
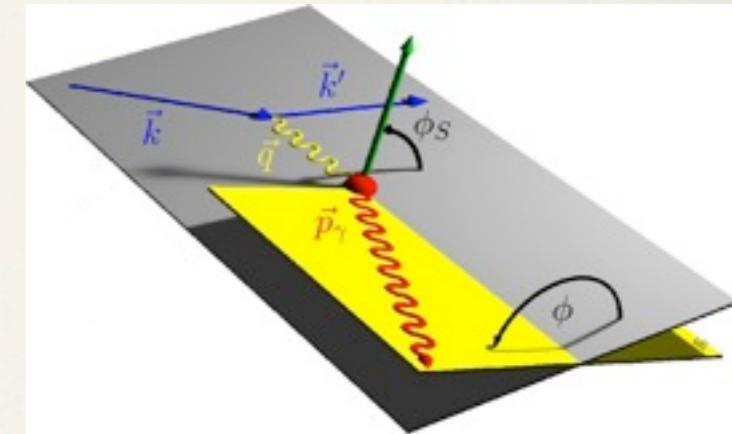
- BH reference amplitude magnifies DVCS
- Measure magnitude  $A$  **and** phase  $\varphi$

of DVCS amplitude  $\mathbf{\tau}_{\text{DVCS}} = A e^{i\varphi}$

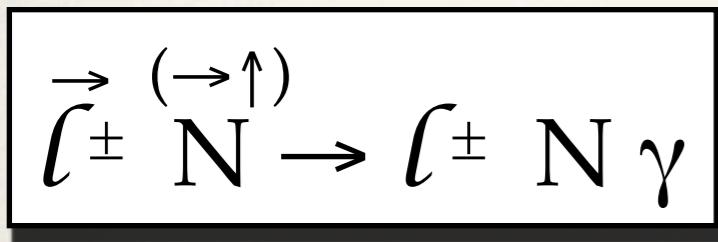
# DVCS @ fixed target experiments



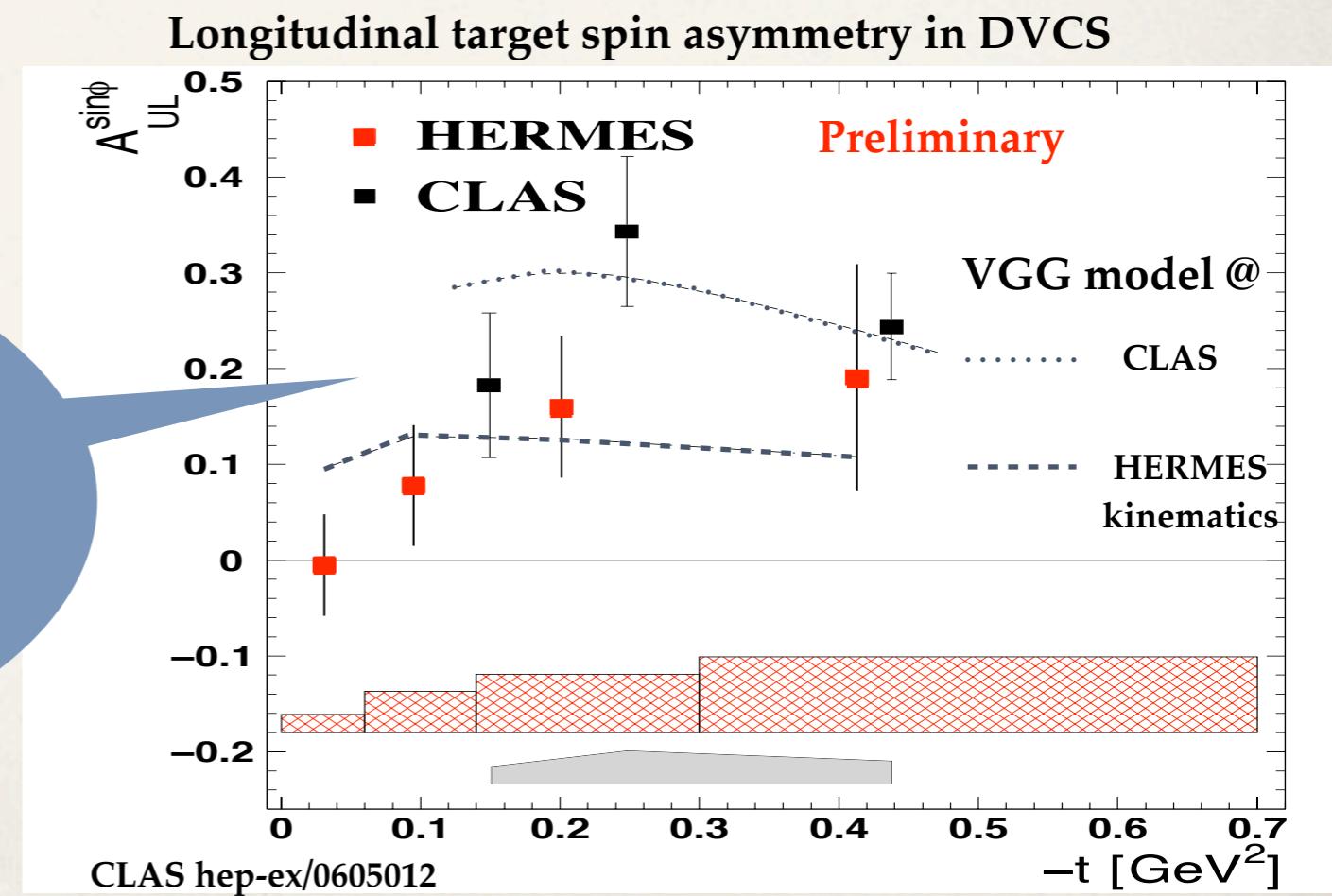
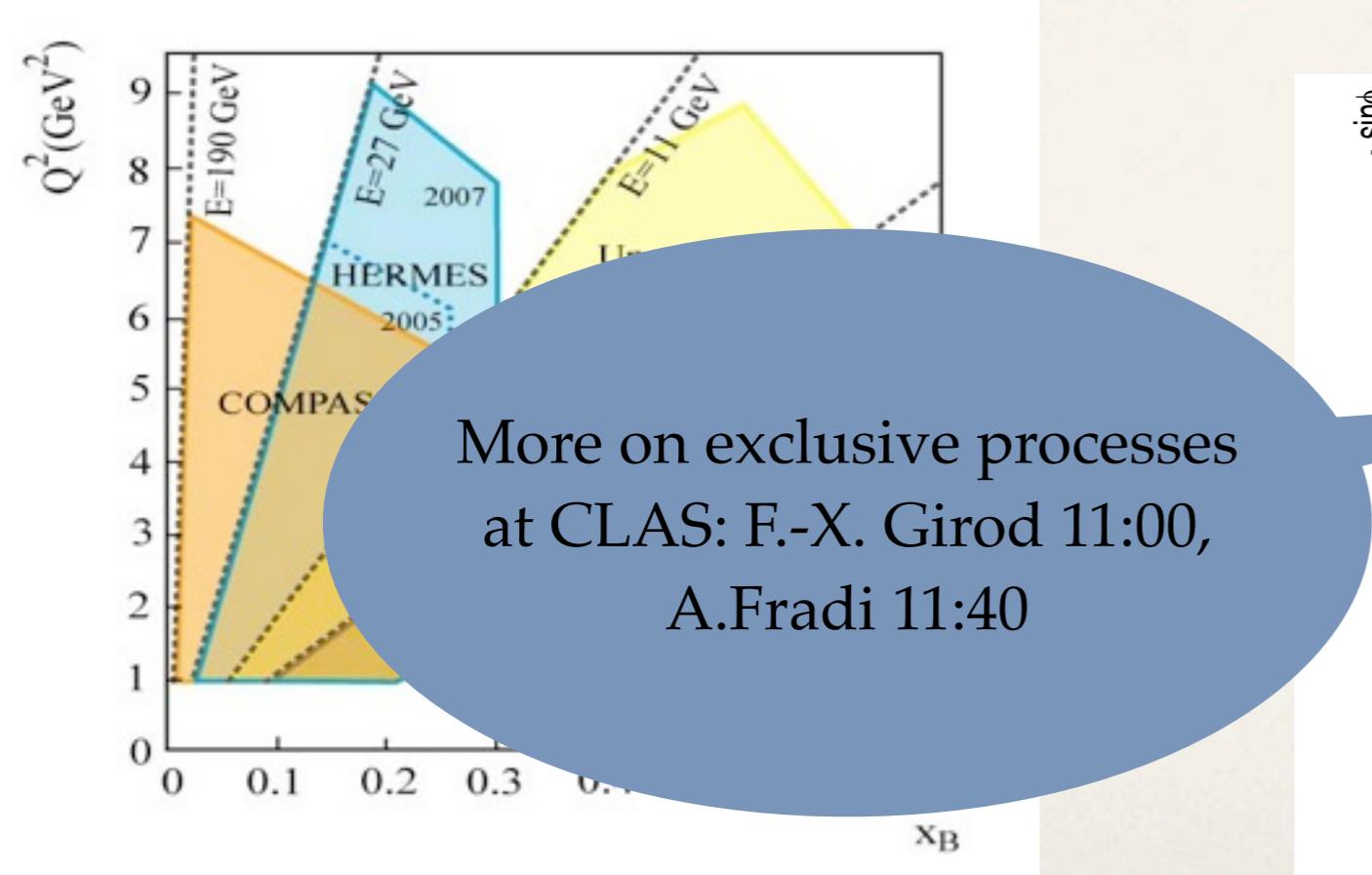
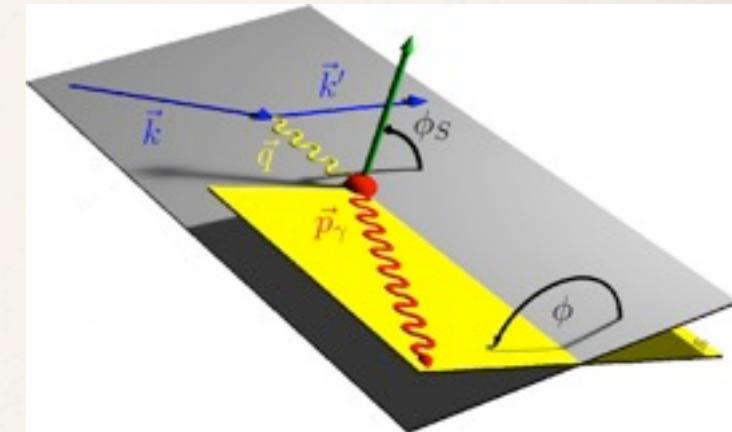
The data are subject to  
a harmonic fit w.r.t. the azimuthal  
angle(s)  $\phi$  (and  $\phi_s$ )  
to obtain **azimuthal asymmetries**



# DVCS @ fixed target experiments



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a harmonic fit w.r.t. the azimuthal  
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# DVCS cross-section in the valence quark region

- Hall-A at JLab, proton target

**Helicity-dependent**

$$\propto \text{Im}(\mathcal{T})$$

GPDs @  $x=\xi$

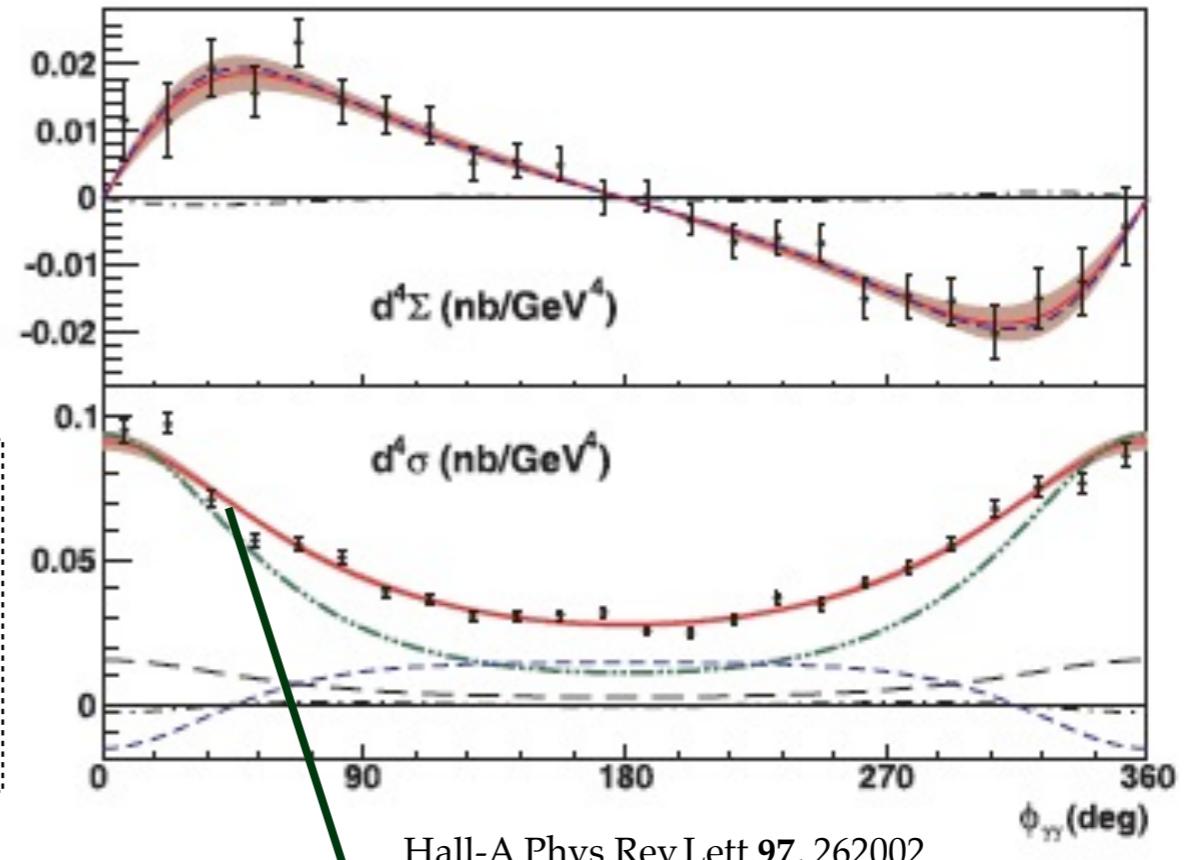
**Helicity-independent**

$$\propto \text{Re}(\mathcal{T})$$

integral of GPDs over  $x$

**Differential cross section vs. azimuthal angle**

Bin:  $\langle x_B \rangle = 0.36, \langle Q^2 \rangle = 2.3 \text{ GeV}^2, \langle t \rangle = -0.28 \text{ GeV}^2$



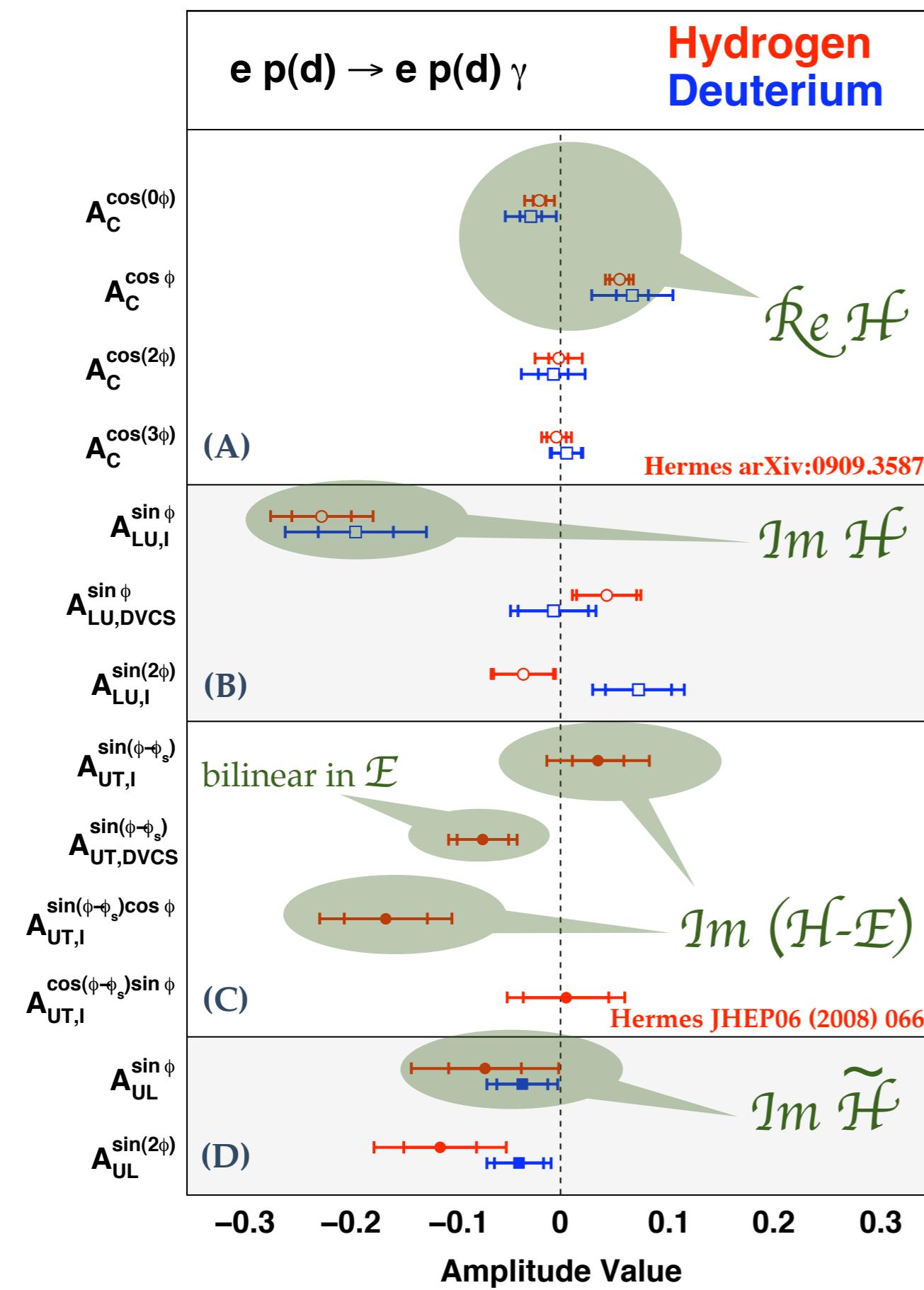
- No  $Q^2$  dependence of  $\text{Im}(\mathcal{T})$

- Indication of factorization down to  $Q^2=2 \text{ GeV}^2$
- GPDs accessible at moderate  $Q^2$

Computed BH contribution  
< helicity-independent cross section

# DVCS azimuthal amplitudes

**HERMES  
(prelim.)**



(A) Beam charge asymmetry:  
**GPD H**

$\Re(\tau_{DVCS})$

↑  
Projects out

(B) Beam helicity asymmetry:  
**GPD H**

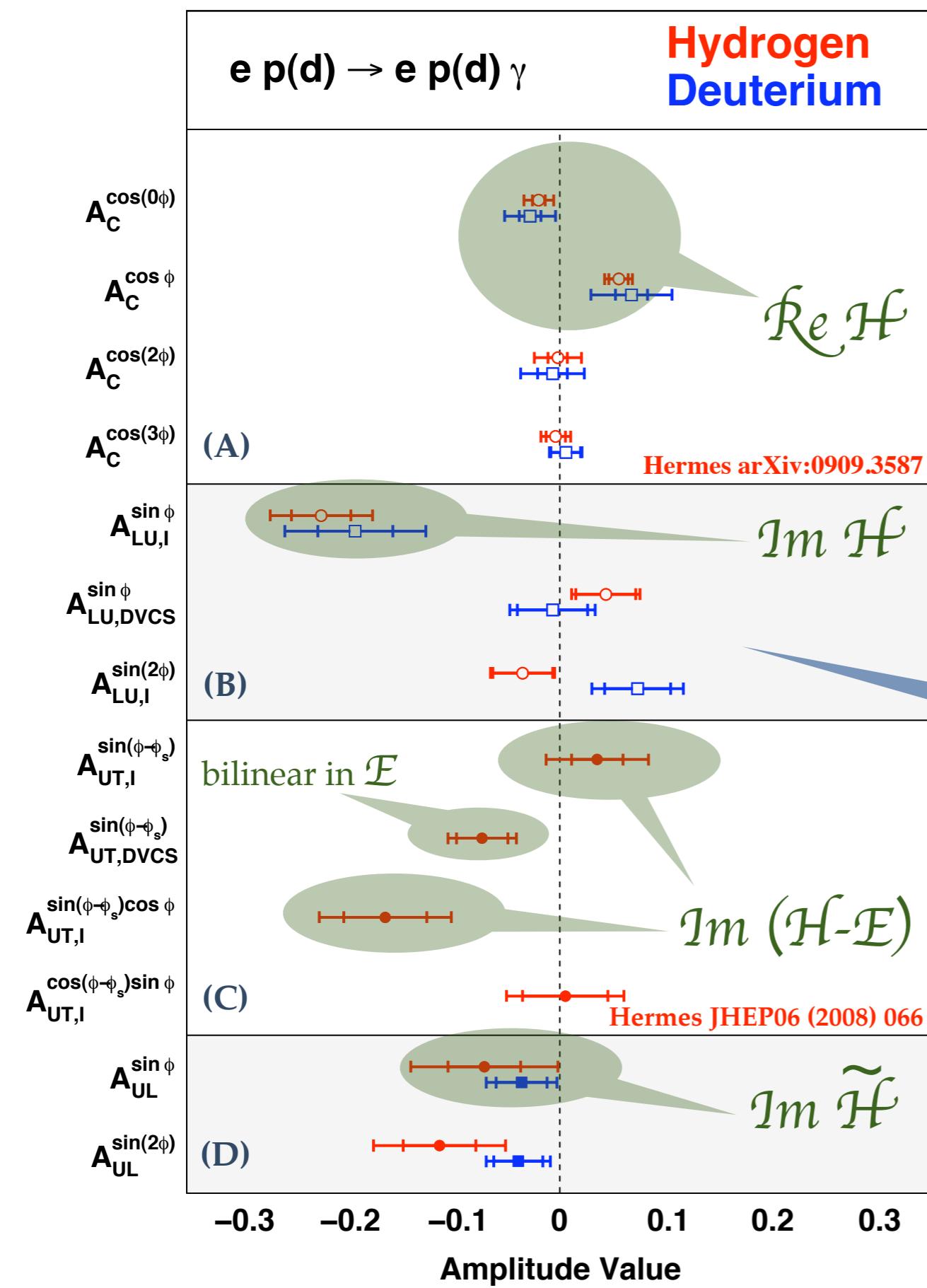
$\Im(\tau_{DVCS})$

(C) Transverse target spin asymmetry:  
**GPD E from proton target**

(D) Longitudinal target spin asymmetry:  
**GPD  $\tilde{H}$**

# DVCS azimuthal amplitudes

**HERMES  
(prelim.)**



(A) Beam charge asymmetry:  
**GPD H**

(B) Beam helicity asymmetry:  
**GPD H**

(C) Transv.  
**GPD E<sub>11</sub>**

(D) Longitudinal target spin asymmetry:  
**GPD  $\tilde{H}$**

$\Re(\tau_{\text{DVCS}})$

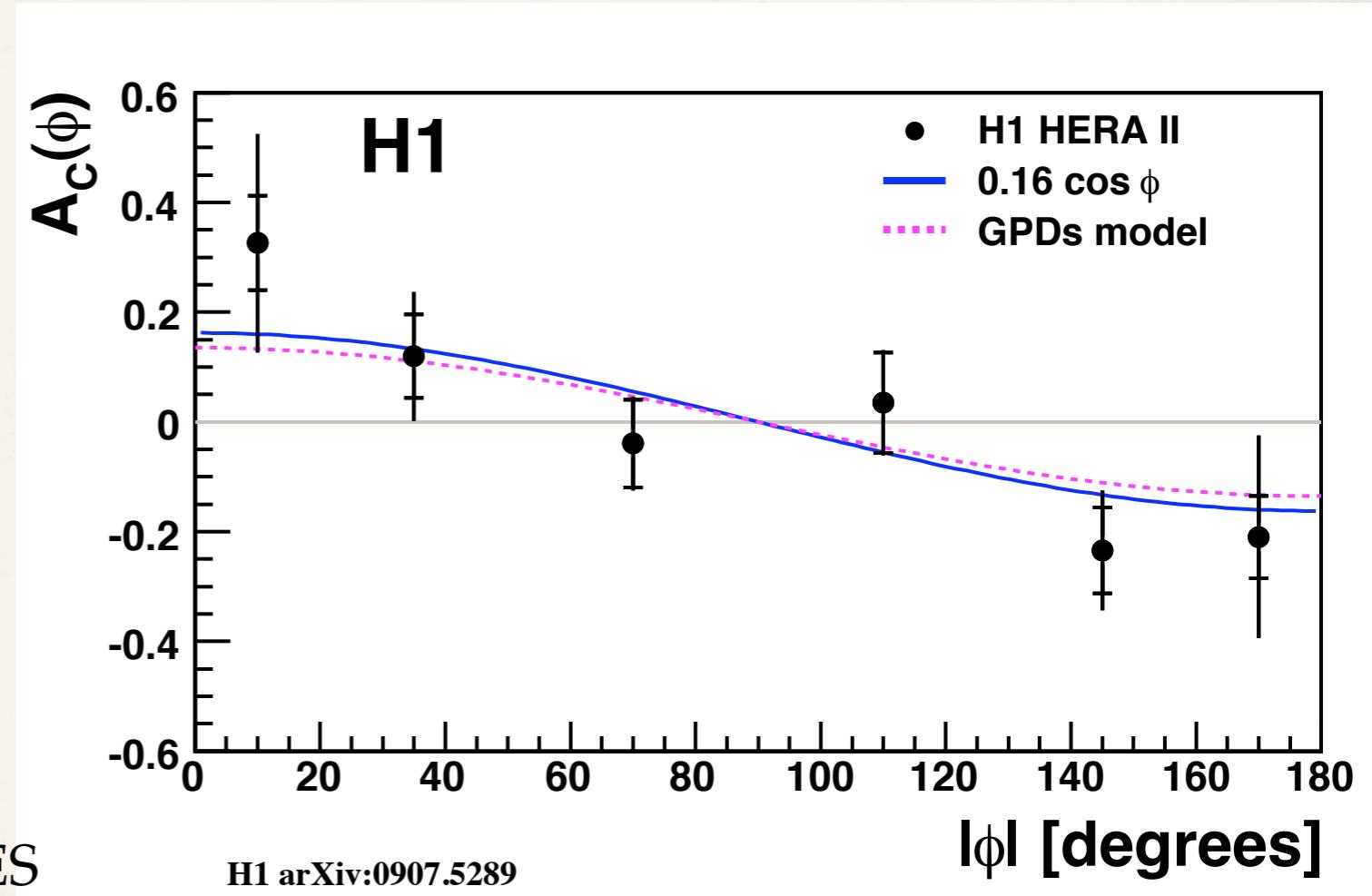
↑  
Projects out

↓  
 $\Im(\tau_{\text{DVCS}})$

Details by  
A. Mussgiller 11:20  
& HERMES Recoil  
detector 2006/07

# HERA / H1: Beam Charge Asymmetry in DVCS

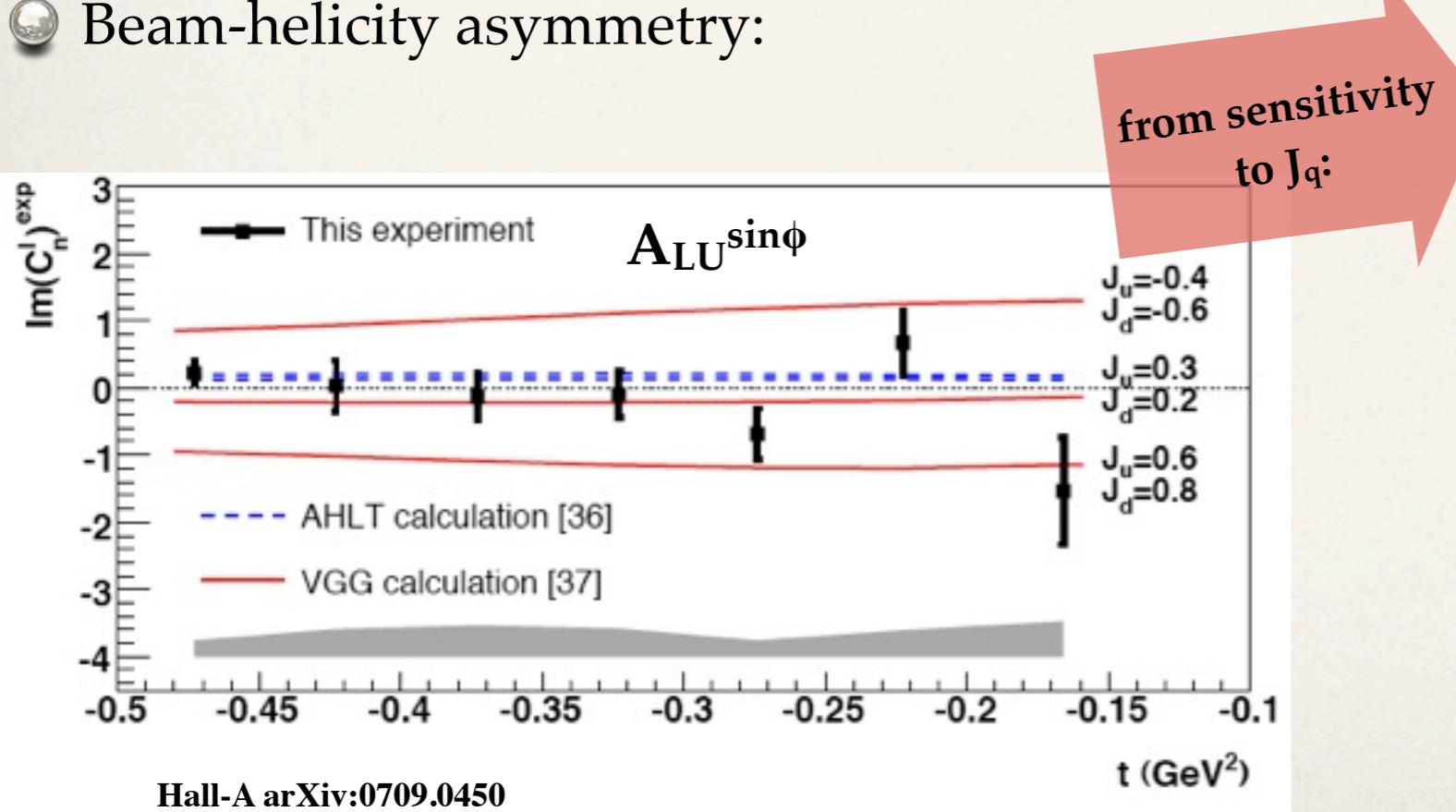
- First measurement at collider
  - low  $x_B = 10^{-4} \dots 10^{-2}$
  - $6.5 < Q^2 < 80 \text{ GeV}^2$
  - $30 < W < 140 \text{ GeV}$
  - $|t| < 1 \text{ GeV}^2$
- Positive  $\cos\phi$  amplitude
  - $\text{Re}(\tau_{\text{DVCS}}) > 0$
  - Sign change compared to HERMES



- Ratio  $\varrho = \text{Re}(\tau_{\text{DVCS}}) / \text{Im}(\tau_{\text{DVCS}})$ 
  - $\varrho = 0.20 \pm 0.05(\text{stat}) \pm 0.08(\text{sys})$
  - In good agreement with calculation from dispersion relation

# Access to the total angular momentum of quarks

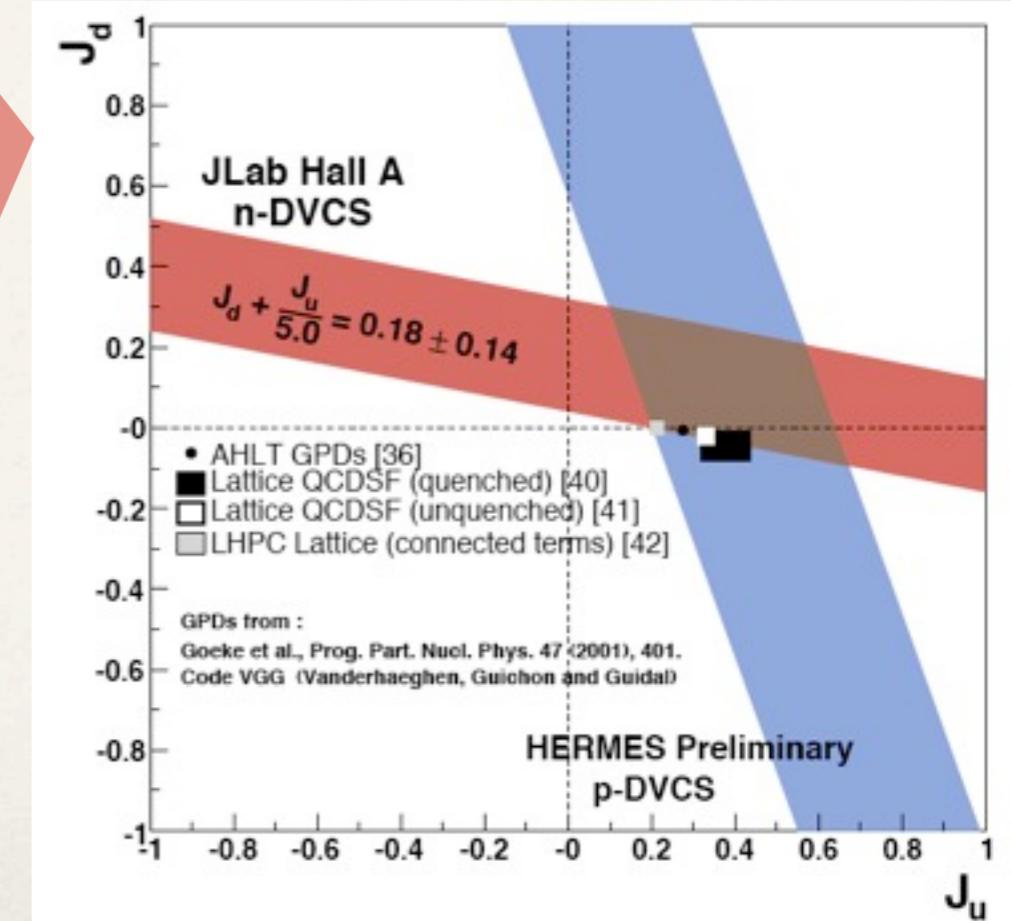
- Hall-A at JLab, deuteron target
- Quasi-elastic proton contribution subtracted from deuteron signal
- Beam-helicity asymmetry:



$\vec{e^- n} \rightarrow e^- n \gamma$ : sensitive to GPD  $E_q$

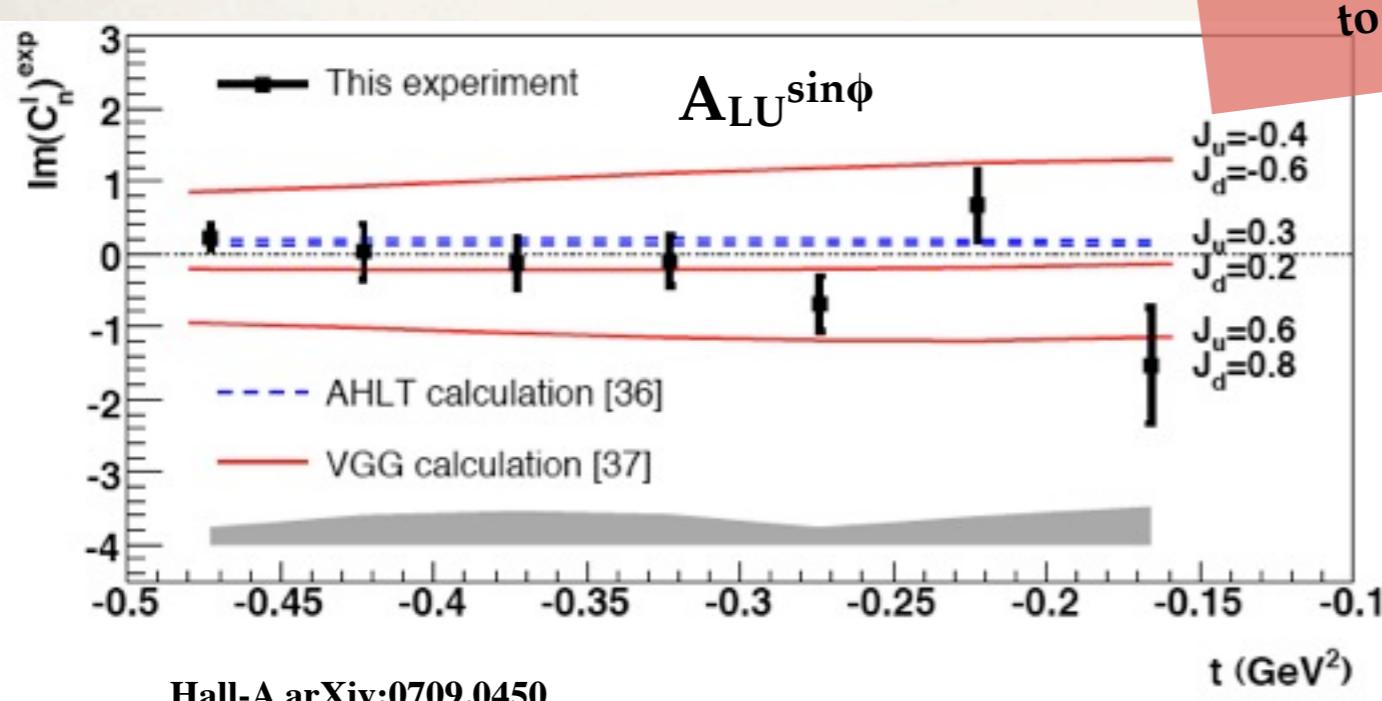
Total angular momentum of quarks  $J_q$ :

$$J_q = \frac{1}{2} \lim_{t \rightarrow 0} \int_{-1}^1 dx x [H^q(x, \xi, t) + E^q(x, \xi, t)]$$



# Access to the total angular momentum of quarks

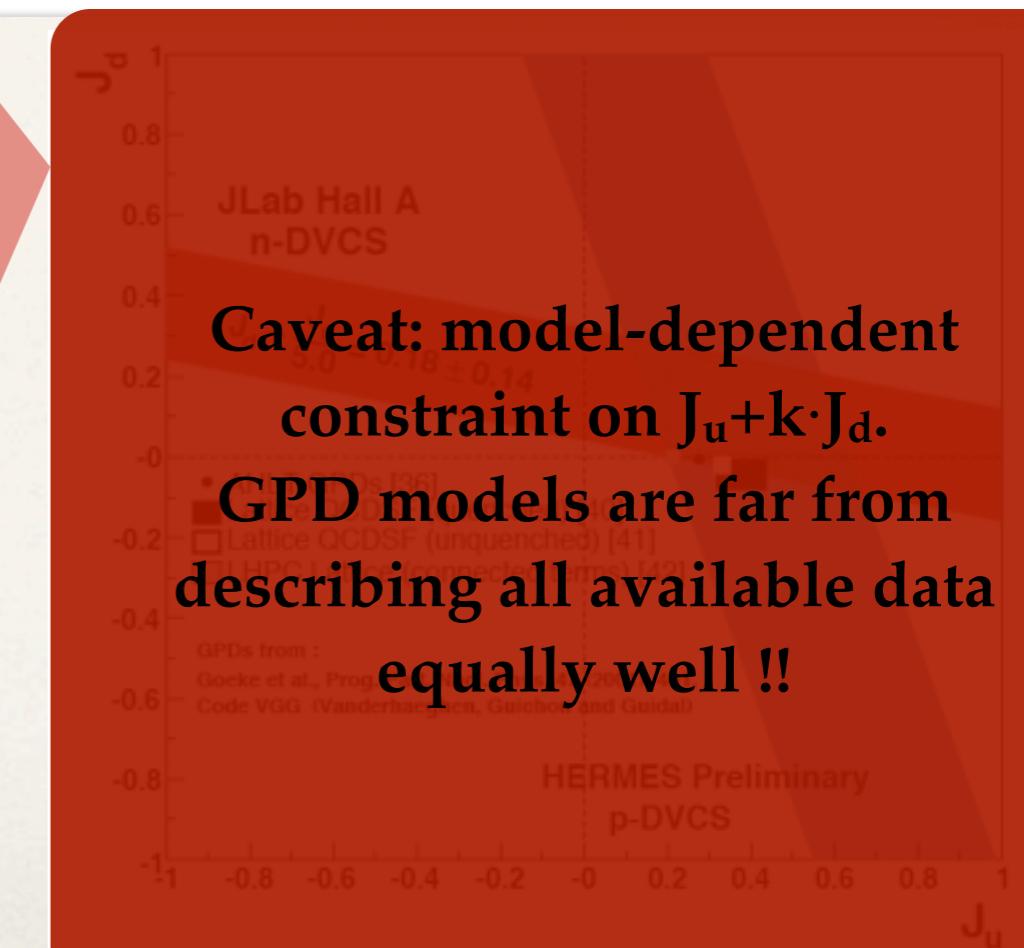
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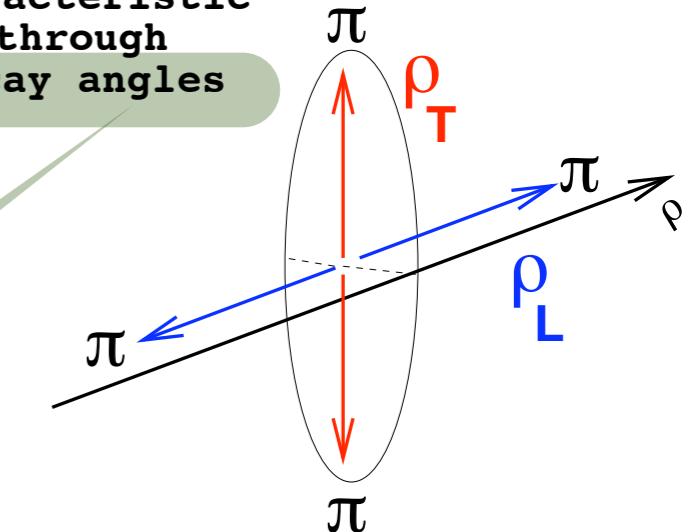
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# $\varrho^0$ Spin Density Matrix Elements

self-analyzing characteristic through decay angles



- Cross-section for exclusive  $\varrho^0$  lepto production:

$$\frac{d\sigma}{dx_B dQ^2 dt} W(x_B, Q^2, t, \phi, \phi_S, \varphi, \vartheta)$$

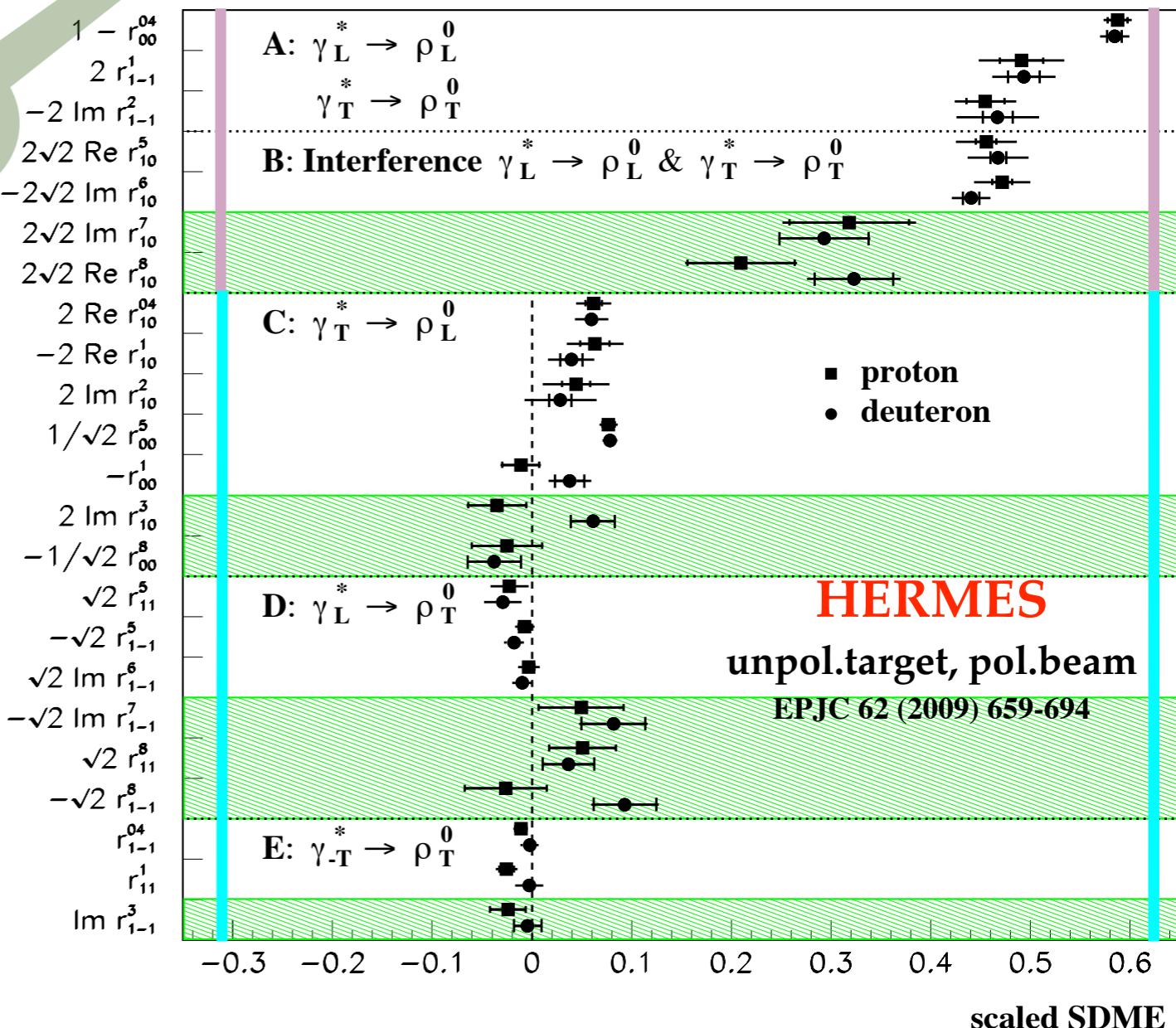
- W parametrized by **Spin Density Matrix Elements (SDMEs)**

- SDMEs describe **helicity transfer** from the  $\gamma^*$  to the  $\varrho^0$ :

s-channel helicity conservation (SCHC)  $L \rightarrow L, T \rightarrow T$

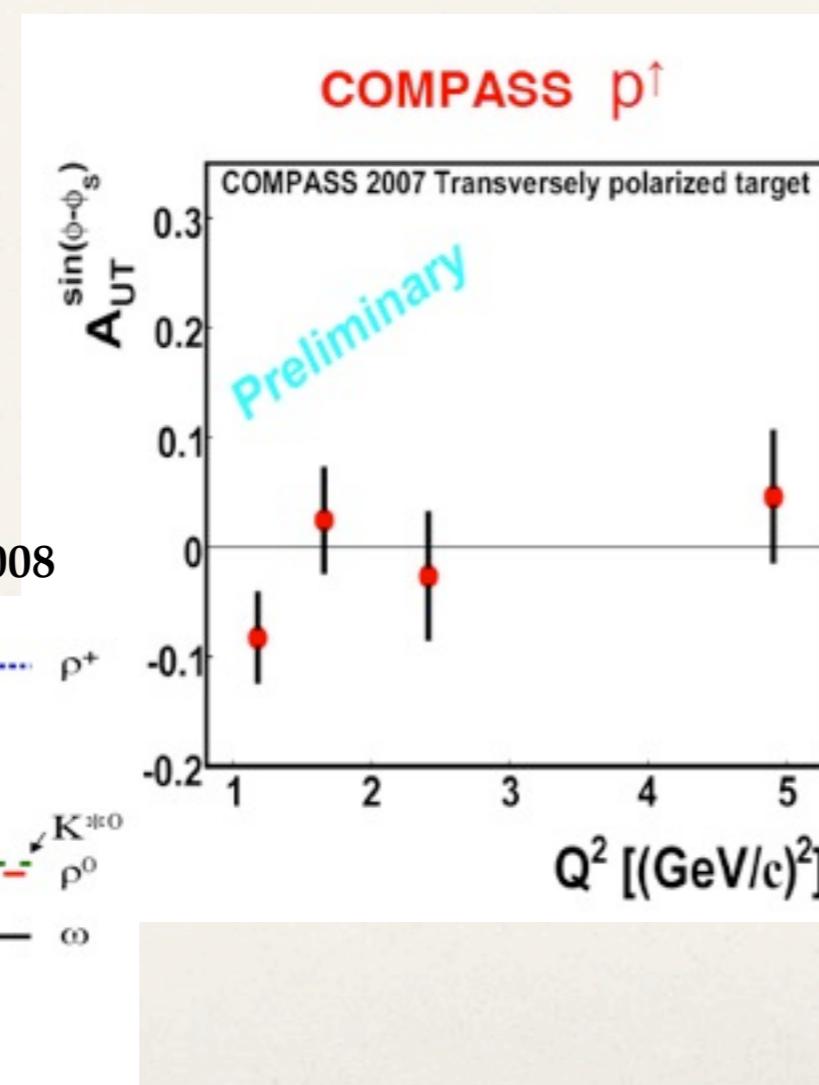
s-channel helicity violation

- More precision data from HERA

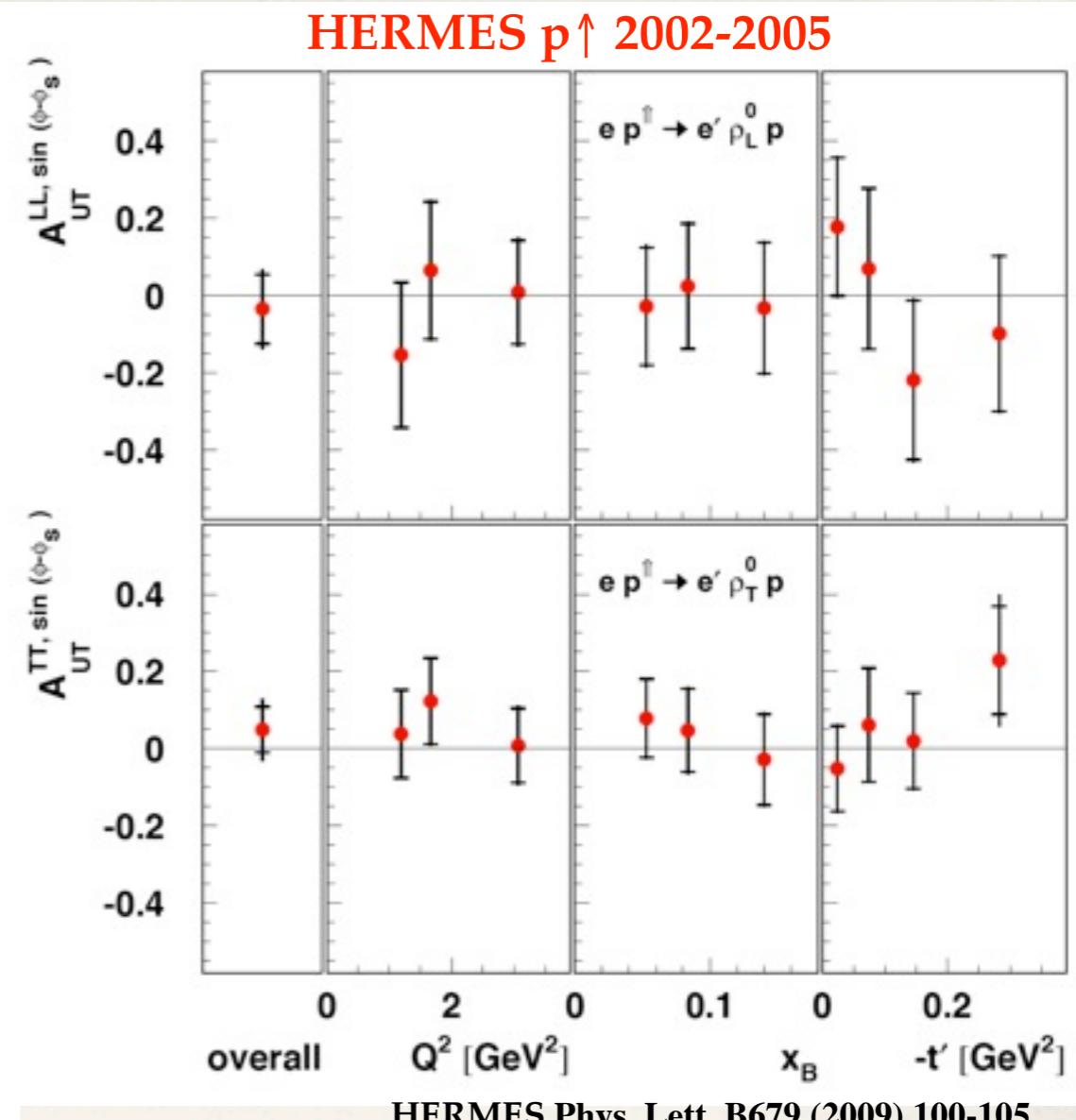
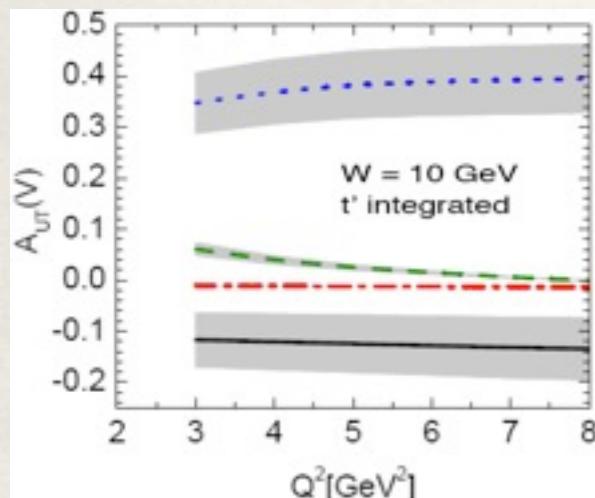


# $A_{UT}$ in $e p^\uparrow \rightarrow e p \rho^0$

- $A_{UT}$ : depends linearly on GPDs ( $E_q + E_g$ ), no suppression w.r.t. GPD H



GPDs: Goloskokov, Kroll 2008



HERMES Phys. Lett. B679 (2009) 100-105

## Exclusive $\omega$ $A_{UT}$

- u- and d-quarks in GPD E do not cancel:  

$$A_{UT} \propto \Im m \left[ (2E^u - E^d) / (2H^u - H^d) \right]$$
 $(\approx -0.10 \text{ expected})$

• HERMES:  $-0.22 \pm 0.16 \pm 0.11$

# The Future

- Global GPD fits

See talk by  
D. Müller  
11:55

- COMPASS 2012-15:

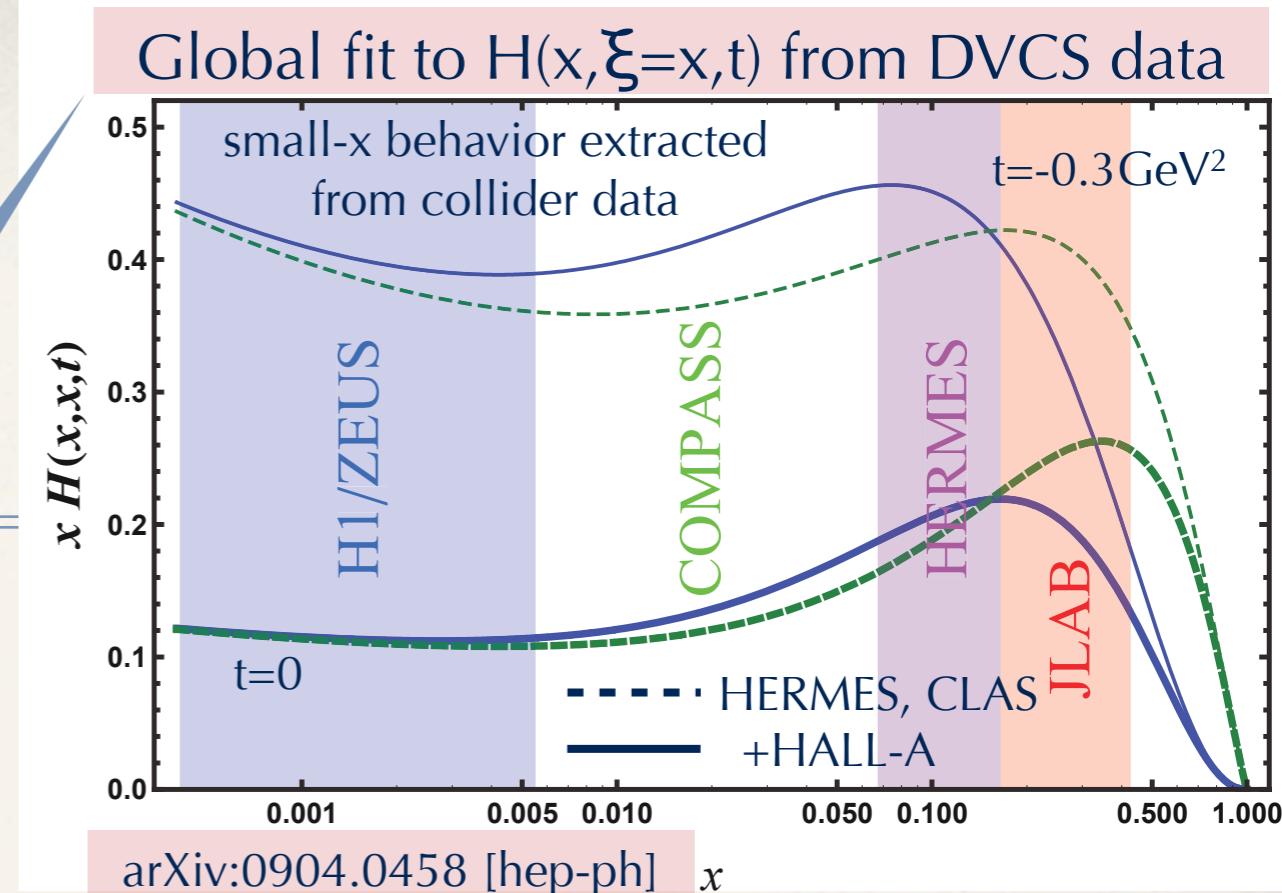
large Recoil + polarized target  
'DVCS test runs' 08/09, small Recoil

- JLab 12 GeV upgrade

- $Q^2_{\max} = 13 \dots 14 \text{ GeV}^2$ ,  $e^+$  beam

- Future Electron-Ion Collider ( $\vec{e}p$  and  $eA$ )

- eRHIC @ BNL:  $\sqrt{s} = 15 \dots 200 \text{ GeV}$  (HERMES: 7 GeV),  
ENC @ GSI:  $\sqrt{s} = 40 \text{ GeV}$ , ...



See talk by N. d'Hose  
Friday afternoon

See EIC workshop  
overview Friday afternoon

# Summary: Hard Exclusive Reactions

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- ➊ Wide spectrum of measurements of cross sections and azimuthal asymmetries
- ➋ Hard exclusive reactions as testing ground for QCD
  - ➌ Universal t slope
- ➌ Access to Generalized Parton Distributions
  - ➍ Different quantum numbers of final state select different GPDs
  - ➎ GPDs provide 3-dimensional picture of nucleons
  - ➏ GPDs allow (in principle) to constrain total angular momentum of quarks

Thanks to everybody who delivered input to this talk!!